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E-2557

Мезоны положительной четности и представления 189

Для представления 189 SU(6) мы обозначим состояние с помощью u = и p = цепи и вычисляем матрицы трансформации, которые соединяют эти две базы. В конце концов мы составляем массовую формулу и коротко обсуждаем одно присоединение частиц.

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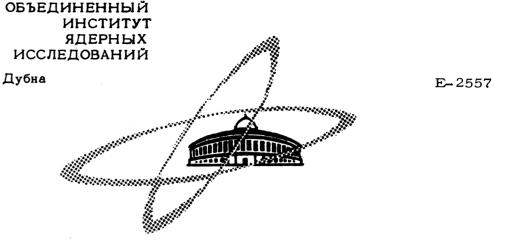
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Plus Parity Mesons and the 189-Plet of SU(6)

For the 189-plet of SU(6) we label the states according to the u-chain and p-chain and calculate the transformation matrices which connect the two bases. Finally we derive a mass formula and discuss briefly a possible particle assignment.

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ААБФРАТОРИЯ ТЕФРЕТИЧЕСКОЙ ФИЗИІ

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PLUS PARITY MESONS AND THE 189-PLET OF SU(6)

1966

1. Introduction

The classification in the SU(6) 189-plet of the positive parity mesons was proposed by Dao Vong Duc, Pham Quy Tu 1 and on the basis of a relativistic extension of SU(6) by Delbourgo and by R. Delbourgo, M.A.Rashid, A.Salam, J.Strathdee 2b/ Using bootstrap ideas R.C.Hwa. S.H.Patil $^{|3|}$ have given arguments in favour of this particle assignment. A more elementary consideration is the following: Assume the low-lying plus parity mesons to be bound states of the 35-plet mesons. Then these bound states are composed of s-, d- and higher states. The p-state and higher odd angular momentum states are parity forbidden. If the s-state is the dominant state, one is allowed to hope that a SU(6) classification is a relevant one. Therefore the plus parity mesons should fit into the Kronecker product 35 x 35. On the other hand using $U(6) \times U(6)$ it is reasonable to value the representation 6×6 and 15×15 as minus and plus parity meson states, respectively. The SU(6) content of 15 x 15 is just 1 + 35 + 189 and this is contained in 35 x 35 indeed. In the following, we restrict ourselves to the 189-plet, having in mind, that the existence and the quantum numbers of some of the recently discovered plus parity mesons seem to be not well established.

2. Labelling of States

Following the ideas of F.Gürsey, A.Pais, L.A. Radicati^{/4/} we use the p-chain (physical chain) and the u-chain (unphysical chain) to get two different systems of basis vectors of the 189-plet. The former will be used to fix the structure of the mass formula, the later one is assumed to give the physical particle states. The p-chain reads $SU(6) \supseteq SU(3) \times (\vec{J}) \supseteq (\vec{J}) \times Y \times (\vec{J})$, where (\vec{T}) denotes the group generated by the generators \vec{T} . Let us concentrate on the 189-plet. One knows the $SU(3) \times (\vec{J})$ content to be $189 = (1,1) + (8,1) + (27,1) + (8,3) + (10,3) + (10^{*},3) + (1,5) + (8,5)$. Therefore we characterize a basis set of states by J^2 , J_3 , I^2 , I_3 , Y and by their SU(3) representation. There remains a degeneracy for the spin one octets so that it is possible to rotate them in the linear space spanned by themselves. The u-chain reads $SU(6) \supseteq SU(4) \times (\vec{S}) \times (\vec{Y}) \supseteq (\vec{N}) \times (\vec{S}) \times (\vec{J}) \times (\vec{Y})$ and we

may fix a basis of the 189-plet by using J², J₃, I², I₃, N², S², Y and C₂. In the 189-plet C₂⁽⁴⁾ is not a function of the other quantum numbers of the u-chain. We consider the u-chain states as particle states. This may be further confirmed by the possibility to give the Y=0 members of them a definite value of the G-parity. The G-parity is calculated as shown in ref.5. In the p-chain decomposition there is a mixture of plus- and minus G-parity states, because the 10-plet is mapped onto the 10*-plet by the G-parity operator. In table I the physical states and their quantum numbers are listed. In table II we have collected the mixing relations between the p- and the u-chain states for the 189-plet according to the matrix scheme. See also ref.1.

p-chain state) = (A) u-chain state).

3. Form of the Mass-Operator

It is rather an unconvenient task, to reduce out the 189×189 Kronecker product, to look for the J = I = Y = 0 members of the occurring octets and last but not least, to discuss which of them should be neglected in order to get a useful mass operator. Therefore we do not give the mass operator in an explicit form but do the following: If M^2 is the operator for the squared masses, we require:

- A. M² is diagonal in the particle states, e.g. in the basis vectors constructed with the aid of the u-chain.
- B. There exist constants a_0 , a_1 , a_2 , a_3 such that $a_0 + a_1 C_2 + a_2 J(J+1) + a_3 \left[I(I+1) \frac{V^2}{4}\right] = (\omega_p, M^2 \omega_p)$

provided ω_{p} is a state of the basis that is constructed with the help of the p-chain.

This however does not fix the operator completely, because the p-chain gives rise to a degenerate system of diagonal operators: It remains to remove the degeneracy of the two J=1 octets. From this we get a new constant which expresses the mixing of these two octets. This parameter is essential for the J=1, I=1/2 mesons. Finally let us stress the fact, that in the p-chain representation only the diagonal terms of M^2 are determined by the requirement B. For the J=1, I=1 mesons this gives rise to a further constant. With the help of the mixing relations we get for the squared masses m_u^2 of the particles (states of the u-chain)

$$m_u^2 = b_0 + b_1 K_1^u + b_2 K_2^u + b_3 K_3^u + b_4 K_4^u + b_5 K_5^u$$

The numbers K_1^u , K_2^u ... are tabulated in table 1,

4. Particle Assignments

To check particle assignments mass relations have been considered, if they are satisfied within 5% in the squared masses.

	Y	I	N	s	J	G	m	
ſ'	0	0	2	0	2	+	1500	
f	0	0	1	1	2	+	1253	
A_2	0	1	1	1	2	_	1324	
к*	1	1/2	3/2	1/2	2		1405	

They have to satisfy the relation (squared masses)

$$4K^* = 2f' + f + A_2$$

which is well established (2%). One and only one place is in the 189-plet for the mesons D and $\rm M_{1}$

	Y	I	N	s	J	G	m
D	0	0	1	1	1	_	1286
M ₁	2	1	0	0	0		1280

With these quantum numbers they should satisfy

$$A_2 + 3D = 2M_1 + 2/9f' + 16/9f$$

which is in good agreement with the experient. Now we are able to calculate (in $(\text{MeV})^2 10^3$)

$$b_0 = 1239$$
, $b_1 = 93$, $b_2 = 75$, $b_3 = -135$.

For this calculation we have used f, f', A2 and D.

For the 35-plet it is well-known, that the determination of the coefficients in the mass formula suffers from large uncertainties (e.g. in the 35-plet a_3

varies between -140 and -150 if determined from the pseudo-vector or pseudo-scalar mesons). The mass values calculated with the help of our b_k 's (look at table 1) are therefore to be considered as rough estimates only. Now let us look at the mesons A_1 and B. If these are actually particles with J=1 the 189-plet offers two possibilities

		Y	I	, N	s	J	G	m
1.	A ₁	0	1	1	1	1	-	1072
	В	0	1	1	0	1	+	1220
2.	A ₁	0	1	1	0	1	-	1072
	в	0	1	О	1	1	+	1220

From both the relations

$$2f' + f + A_1 + 2B = 3D + 3A_2$$

follows, that is satisfied within 1% in the the squared masses! X). Assuming for the resonances K^* (1320) and C the quantum numbers

	Y	I	N	S	J	G	
к	1	1/2	1/2	1/2	0		1320
С	1	3/2	1/2	1/2	1		1215

one gets the relations

$$C + 1/6 \text{ f'} + 7/12 \text{f} = 1/3 (A_1 + 2B) + 3/4 A_2$$

 $9M_1 + 5C + 6D = 11/3 (A_1 + 2B) + 9K^{**}$
 $K^{**} + 1/4 A_2 = M_1 + 19/54 \text{f'} + 11/108 \text{ f.}$

The first is satisfied within 1%, the others within 4%. For the experimental data we have used the table of A.H. Rosenfeld et al⁷. It is a pleasure to thank dr. U. Kundt for interesting discussions on recently discovered resonances.

After this paper was completed we received a preprint of Chia-Hun Chan and Nguyen-Hun Xuong containing the mixing matrices also.

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x) From the well-satisfied relation $^{6)}$ $A_1+A_2=2B$ we obtain $b_2=b_5$ if the assignment 1 is true and $b_1+b_3\cdot 3+b_5=0$ if the other one is correct.

symbol ပ m exp. 2250 1571 1753 1988 1150 1650 1476 1742 1638 m² theor. 1950 1650 1650 1500 1900 1270 1370 1700 1410 2010 1090 2610 840 2320 \mathbf{K}_{5}^{u} $K_4^{\rm u}$ ж. З Table 1, Particle states **K**^u2 00000 -2 55/3 ıı T r + 1 1 + $c_2^{(3)}$ $C_{2}^{(4)}$ S 11424441 z Н × 7 4 4 8

Table II

Transformation matrices

$$J = 2 Y = 0 I = 0$$
 singlet octet
$$J = 1 Y = 0 I = 0$$
 octet a octet b
$$J = 1 Y = 0 I = 0$$
 octet a octet b
$$J = 1 I = 0$$
 octet a octet b
$$J = 1 I = 0$$
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$$J = 1 I = 0$$
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$$J = 1 I = 0$$
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$$J = 1 I = 0$$
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$$J = 1 I = 0$$
 octet a octet b
$$J = 0 I = 0$$
 octet a octet b
$$J = 0 I = 0$$
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$$J = 0 I = 0$$
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$$J = 0 I = 0$$
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$$J = 0 I = 0$$
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Notation: SU(3) plet = (A) N, S, $C_2^{(4)}$

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