UNIVERSITY OF LEIPZIG INSTITUTE FOR THEORETICAL PHYSICS Department: Theory of Elementary Particles

TP2 2015

Lecturer: PD Dr. A. Schiller

List of problems 7

(19. and 20. required, use 21. to collect an additional point)

- 19. A surface charge density $\sigma(\theta) = \sigma_0 \cos \theta$ is glued to the surface of a spherical shell of radius R (σ_0 is a constant and θ is the polar angle). There is a vacuum, with no charges, both inside and outside of the shell. Calculate the electrostatic potential and the electric field vector both inside and outside of the spherical shell.
- 20. A conducting sphere of radius *a* carrying a charge *q* is placed in a uniform electric field \mathbf{E}_0 . Find the potential and the electric field vector at all points inside and outside of the sphere, What is the dipole moment of the induced charge on the sphere?
- 21. Consider a sphere of radius R centered at the origin. Suppose a point charge q is put at the origin and this is the only charge inside or outside the sphere. Furthermore the potential is $\Phi = V_0 \cos \theta$ on the surface of the sphere. What is the electrostatic potential and the electric field vector both inside and outside the sphere?

Hint: Use superposition to take into account the potential of the point charge inside the sphere.