

**UNIVERSITY OF LEIPZIG**  
**INSTITUTE FOR THEORETICAL PHYSICS**  
**Department: Theory of Elementary Particles**

TP3 2017

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List of problems 5

13. Consider the motion of two charged particles (masses  $m_{1,2}$ , charges  $q_{1,2}$ ) in a homogeneous magnetic field given by the constant vector  $\mathbf{B}$ . Find the condition under which the motion of the center of mass and the relative motion become decoupled.

*Hint:* Use  $\mathbf{A} = \frac{1}{2} \mathbf{B} \times \mathbf{r}$ .

14. Find the Hamilton function for an anharmonic oscillator, the Lagrange function of which is given by

$$L = \frac{1}{2} m \dot{x}^2 - \frac{1}{2} m \omega^2 x^2 - \alpha x^3 + \beta x \dot{x}^2.$$

Check that the Hamilton's equations of motion are equivalent to the Lagrange's equation of motion.

15. The Lagrangian for a particle in an external field (described by the potential  $V$ ) in an inertial frame is given by

$$L_0 = \frac{1}{2} m \mathbf{v}_0^2 - V(\mathbf{r}_0)$$

where the subscripts  $_0$  denote the inertial frame.

Consider a frame of reference rotating with constant angular velocity  $\boldsymbol{\Omega}$ . Denote all vectors in that frame by vectors without subscripts (e.g.  $\mathbf{r}_0 \rightarrow \mathbf{r}$ ). Find the Hamiltonian for the particle in that frame.

Check that the corresponding Hamilton's equations are equivalent to the equation of motion for a particle in that rotating frame.