

Does KPZ describe pushed interfaces with quenched disorder?

CompPhys18

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Outline:

- **Kardar-Parisi-Zhang:**
Recent successes for $d = 2$ (i.e., $1 + 1$)
versus stagnation for $d > 2$
- **Frozen disorder: rough interfaces & percolation:**
Generalized percolation, $T = 0$ RFIM, "minimal model"
- $d = 2$
- **Morphological phase transitions for supercritical percolation:**
Sponge phases
 - Bond percolation, $3 \leq d \leq 6$
 - GEP
- **KPZ for non-spongy transition in $d = 3$?**

KPZ:

Driven interfaces with **annealed** noise

Critical exponent known exactly in $d = 2$ ($1 - d$ interfaces)

Scaling functions also known exactly in $d = 2$

$d > 2$: exponents known approximately; upper critical dimension = ?

Experimental verification:

- Old experiments (< 2000): uncontrolled mix of annealed & quenched noise:
burning cigarette paper, coffee filter wetting, wetting in sponges, magnetic domain propagation, ...
→ no clear conclusions
- Takeuchi et al., 2010:
very well controlled;
 $d = 2$
→ everything ok.

Frozen disorder:

Interfaces can get **pinned** !

Critically pinned interfaces:

- Fractal: percolation
- non-fractal but rough: self-affine

Transitions between both observed since 1980's:

Robbins, Cieplak, Ji, Martys, Koiller, ...

- Small surface tension in fluid imbibition, large disorder in RFIM: $\rightarrow$ fractal
- High surface tension, small disorder: $\rightarrow$ rough surfaces

But little deeper understanding

Generalized Epidemic Process (GEP)

H.-K. Janssen et al., 2004

$p_k = \text{prob}\{\text{site gets infected (wetted) during } k\text{-th attack}\}$

$q_k = q_{k-1} + (1 - q_{k-1})p_k = \text{prob}\{\text{site is infected after } k\text{-th attack}\}$

Critical interface is non-fractal, if p_k increases sufficiently with k

Transition fractal $\leftrightarrow$ non-fractal is **tricritical point**

Special GEP's:

- T=0 RFIM without spontaneous nucleation:

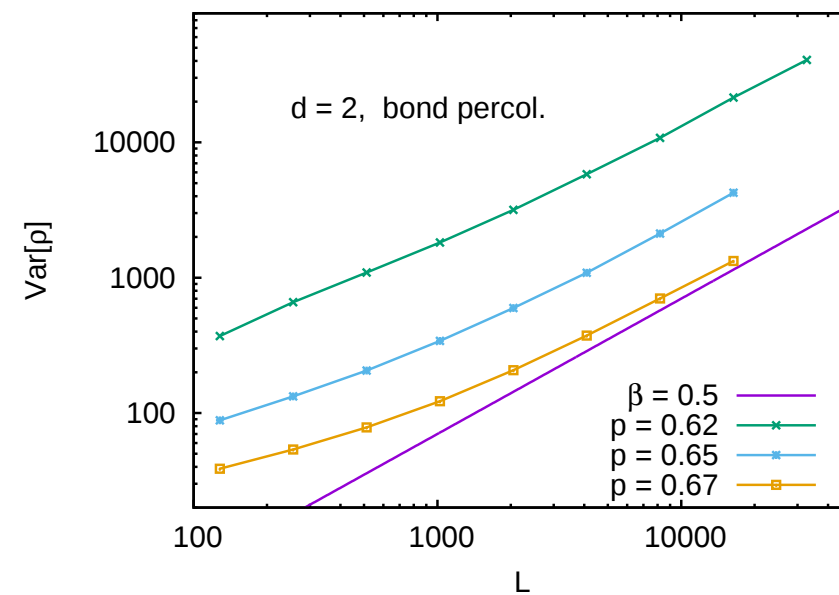
Spins flip, when neighboring spins have flipped $p_k = \text{prob}\{\text{neighbor flipping pushes local magnetic field above/below zero}\}$

- “Minimal model”: $p_2 \neq p_1$, but $p_k = p_2$ for $k > 2$

All following results are for minimal model, but all tests with other versions show universal behavior

$d = 2$:

- Critically pinned interfaces are **always** in percolation universality class (P. Grassberger, arXiv:1711.02904; PRL 2017)
- Supercritical GEP $\sim$ KPZ



Morphological phase transitions for supercritical percolation:

Site percol., $d \geq 3$:

$$p_c < 1/2$$

→ for $p_c < p < 1 - p_c$, there exist co-existing ∞ clusters
(wetted & non-wetted sites both percolate)

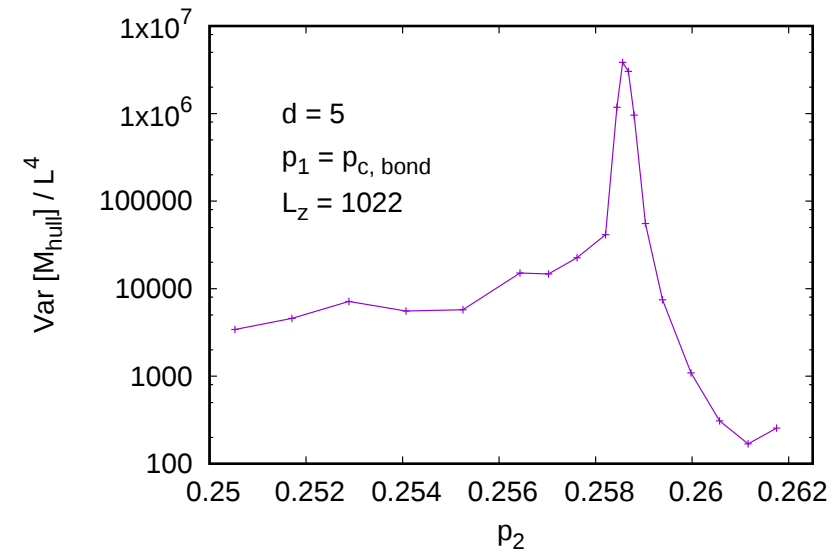
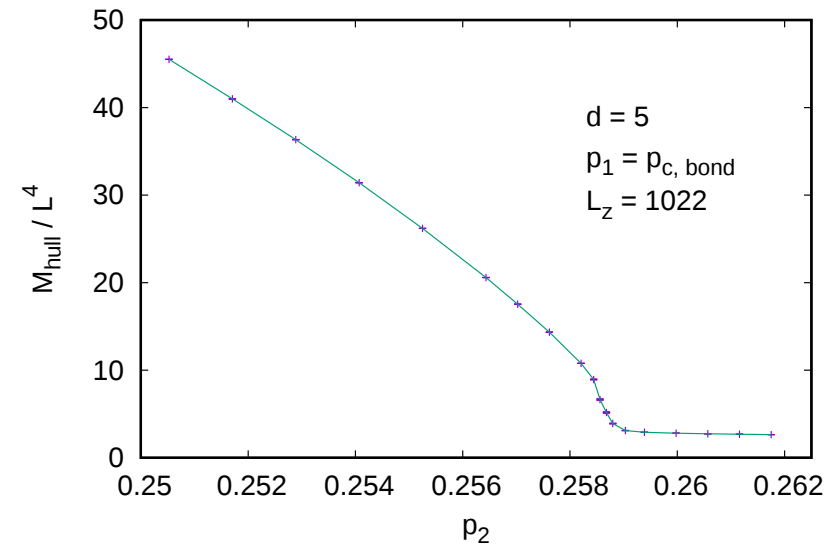
Is this also true for

- bond percolation?
- for GEP?

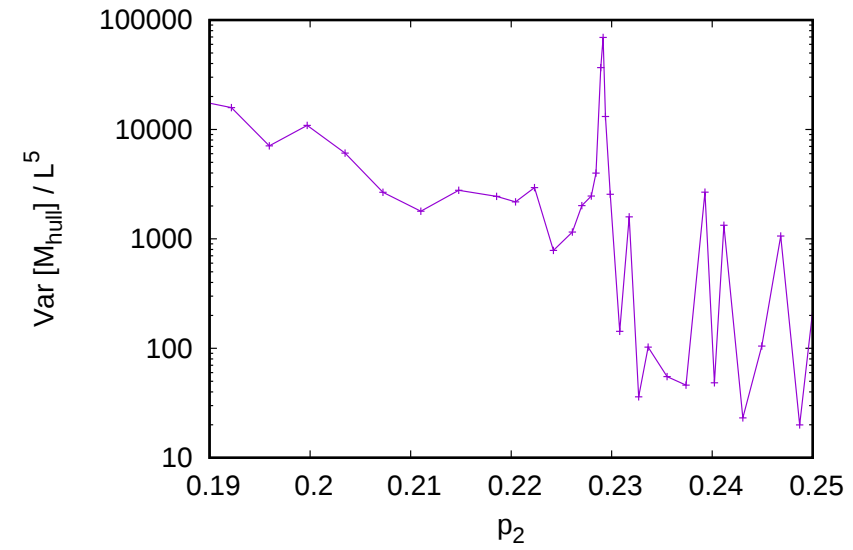
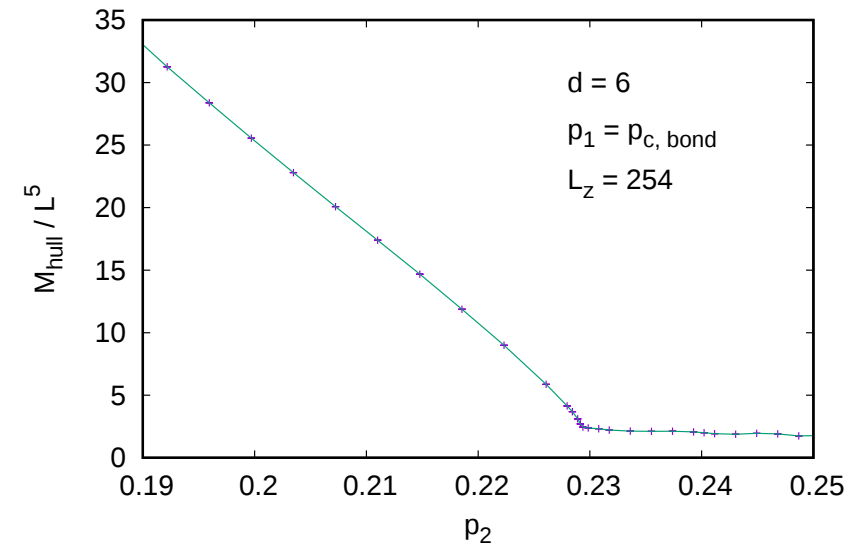
Simulations:

- Hyperplane seed:
start with entire L^{d-1} “bottom hyperplane” of d –dimensional lattice infected
- Spread the epidemic into region $z > 0$, with periodic lateral b.c.
- Stop epidemic just before top hyperplane $z = L_z$ is reached
- Starting from top hyperplane, find the hull of th infected cluster by means of (depth-first) recursive hull-walking algorithm
- How far does hull reach down?
Are there “fjords” or “channels” in where hull reaches down to bottom?
Average hull mass =?

$d = 5$, bond percolation:



$d = 6$, bond percolation:



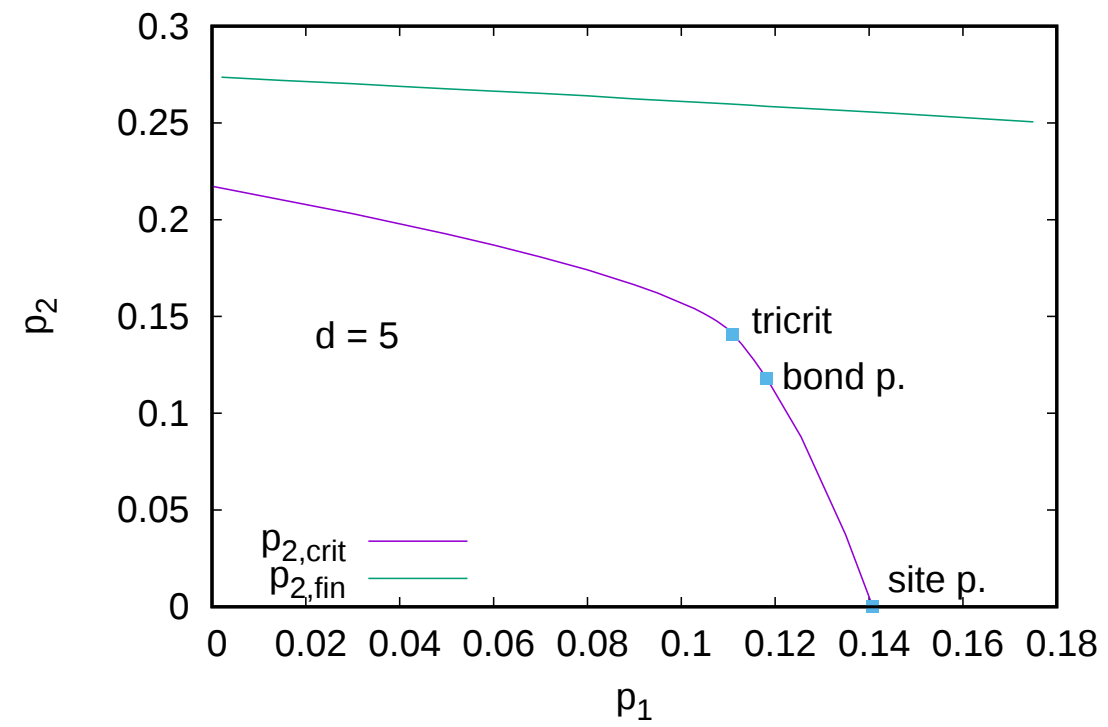
Thresholds for spongy clusters at bond percolation:

d	$p_{\{\text{inf}\}}$	$p_{\{\text{fin}\}} / p_c$
3	0.3605(10)	1.449
4	0.2987(10)	1.865
5	0.2586(5)	2.188
6	0.2291(5)	2.432

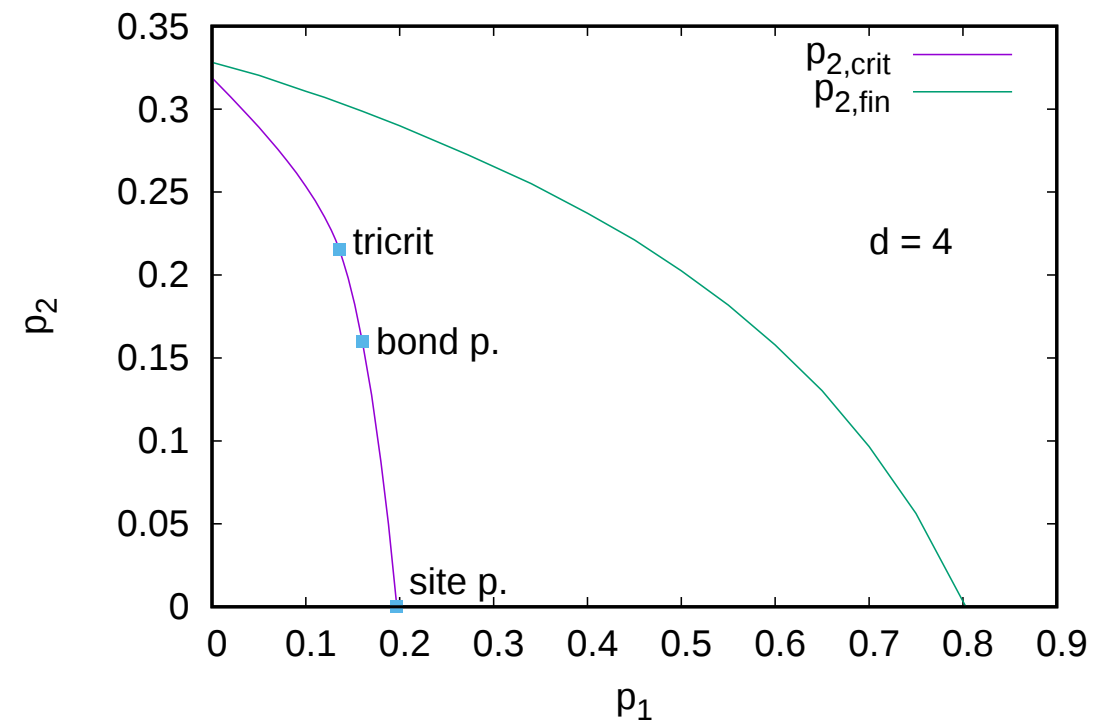
B. Bock et al., aXiv:1811.01678 (2018):

- Existence of multiple supercritical bond percolation clusters proven for $d \geq 8$
- $p_{inf} > \log(d)/2d$ for large d

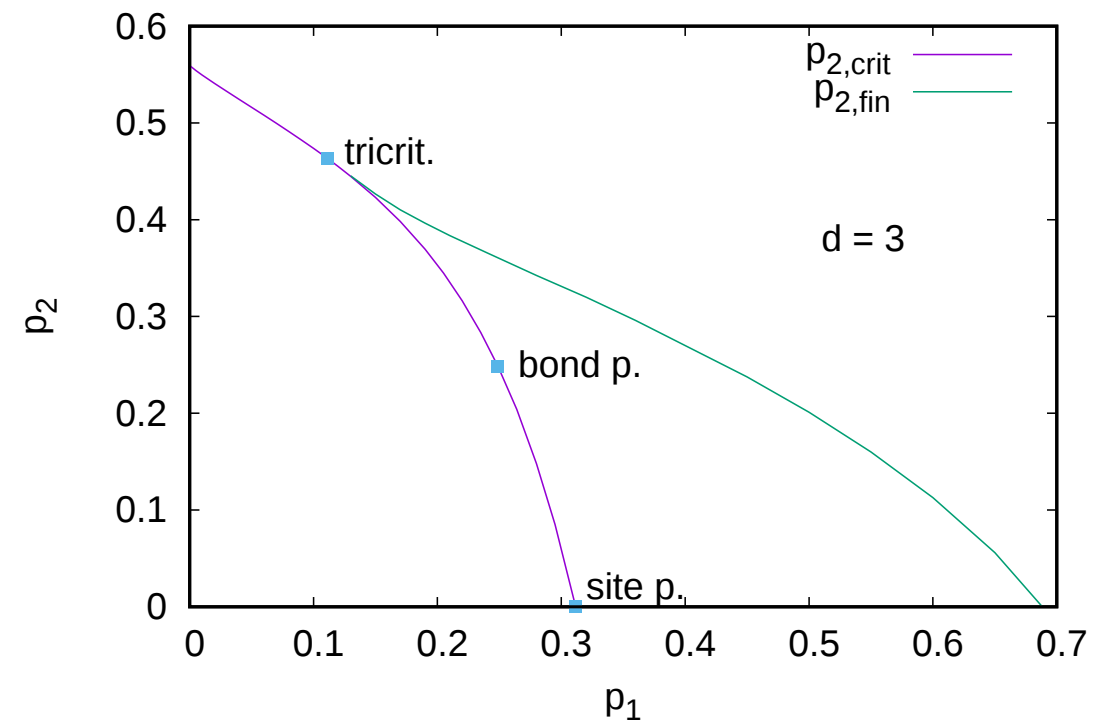
$d = 5$, minimal model GEP:



$d = 4$, minimal model GEP:

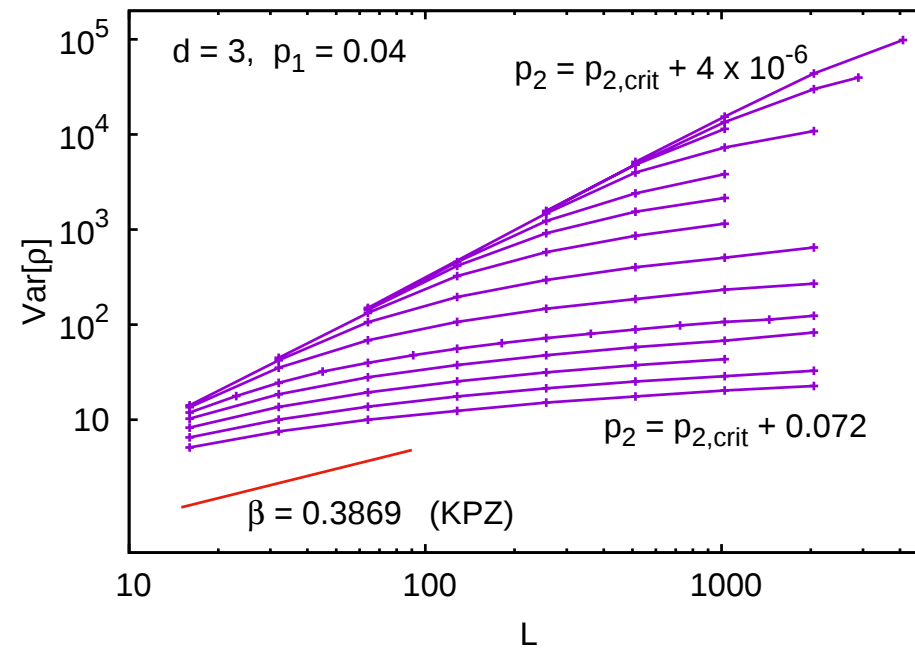


$d = 3$, minimal model GEP:

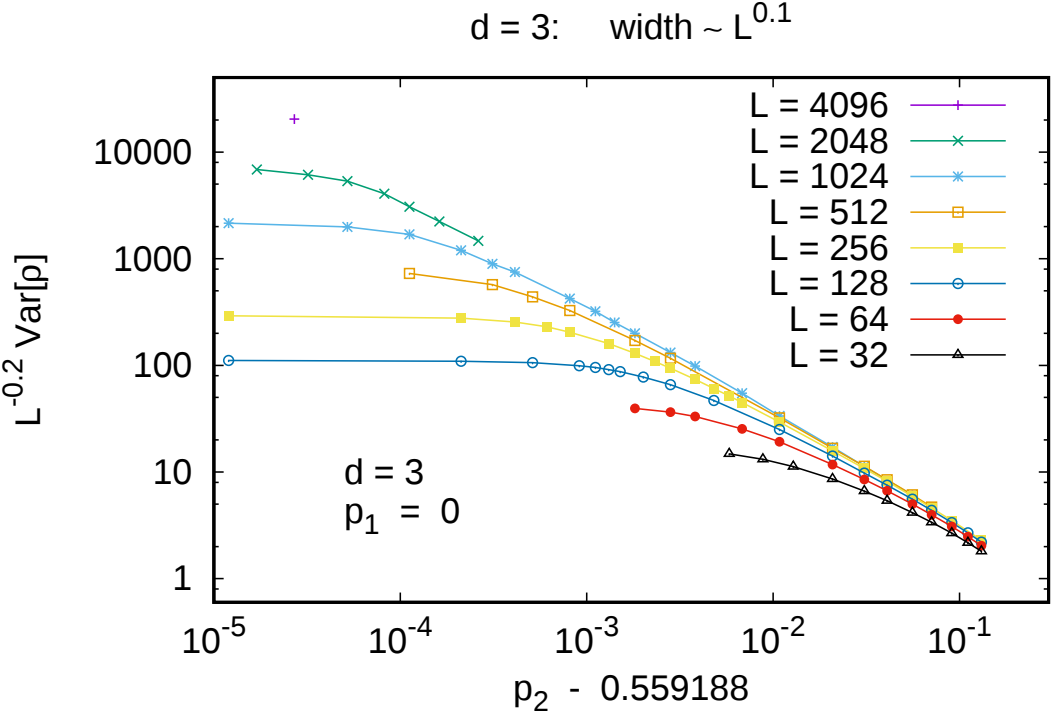


- In spongy phase, obviously no KPZ scaling
- KPZ in compact (non-spongy) phase?

$d = 3$, minimal model GEP with $p_1 = 0.04$:



Similar for $p_1 = 0$:



Conclusions:

- Existence of multiple coexisting supercritical clusters:
→ “spongy” phases, where clusters penetrate each other
- Transition spongy $\leftrightarrow$ compact is a true (2nd order?) phase transition, at least for $3 \leq d < 6$
- For $d = 6$ is transition more complex?
- Even in compact (non-spongy) phase, interfaces in $d = 3$ are NOT in KPZ universality class
- $d = 2$:
 - No fractal $\leftrightarrow$ nonfractal transition for critical surfaces
 - supercritical surfaces are KPZ