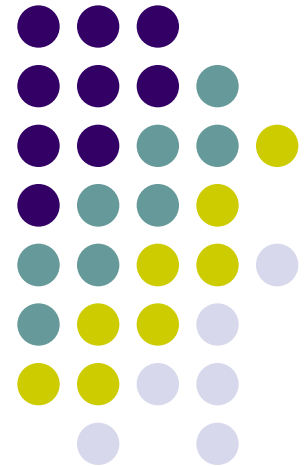


# Wang-Landau type Monte Carlo study of crystallization in melts of short semi-flexible polymers

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**Timur Shakirov**

University of Halle



# Computational model

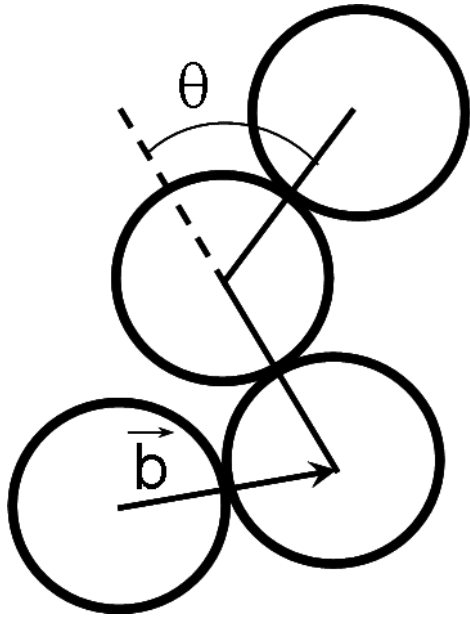


Hard spheres

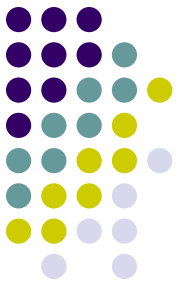
+

$$U(\theta) = \begin{cases} -\varepsilon & \theta < \theta_{\max} \\ 0 & \theta > \theta_{\max} \end{cases}$$

$$0 \leq \theta \leq 120^\circ$$



# Computational model

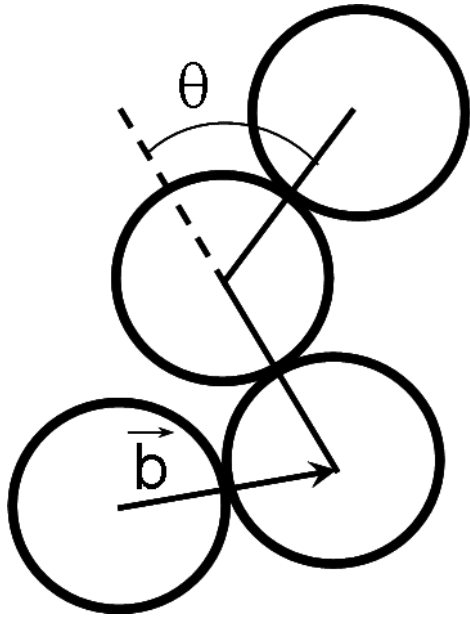


Hard spheres

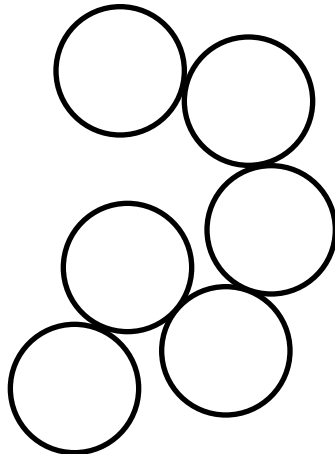
+

$$U(\theta) = \begin{cases} -\varepsilon & \theta < \theta_{\max} \\ 0 & \theta > \theta_{\max} \end{cases}$$

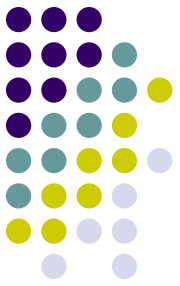
$$0 \leq \theta \leq 120^\circ$$



High Energies



# Computational model

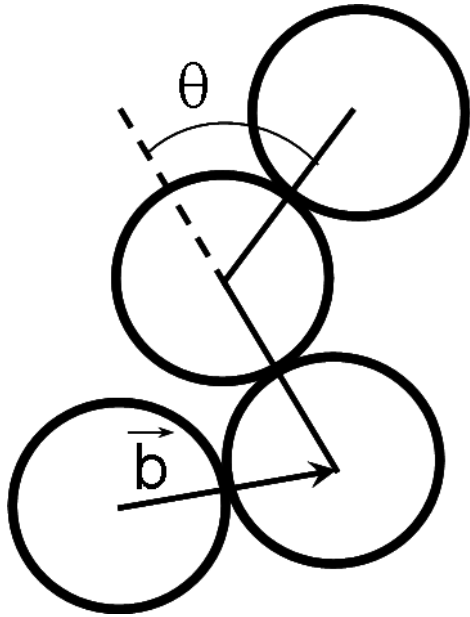


Hard spheres

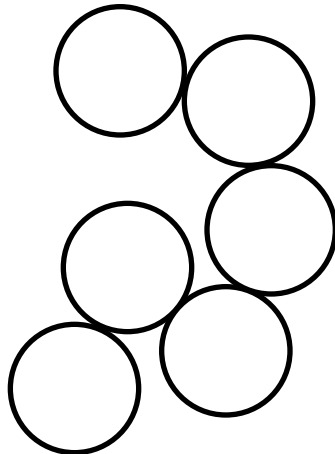
+

$$U(\theta) = \begin{cases} -\varepsilon & \theta < \theta_{\max} \\ 0 & \theta > \theta_{\max} \end{cases}$$

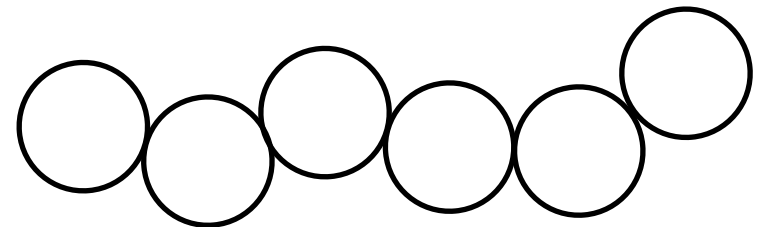
$$0 \leq \theta \leq 120^\circ$$



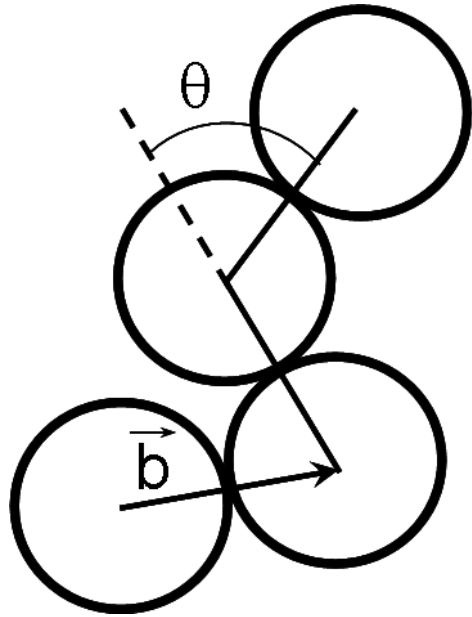
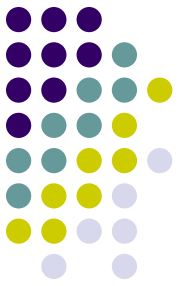
High Energies



Low Energies



# Computational model



Hard spheres

+

$$U(\theta) = \begin{cases} -\varepsilon & \theta < \theta_{\max} \\ 0 & \theta > \theta_{\max} \end{cases}$$

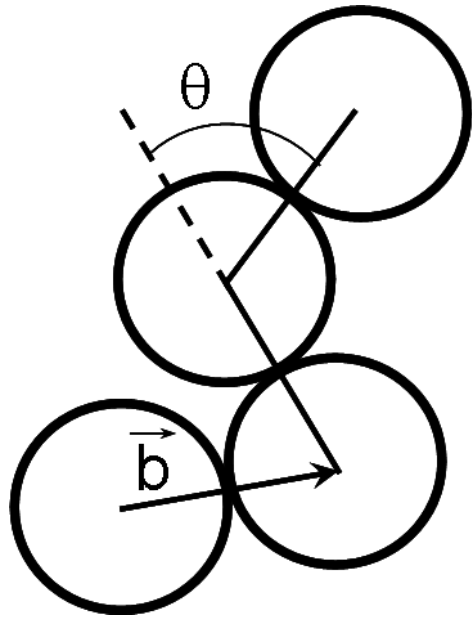
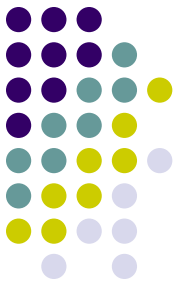
$$0 \leq \theta \leq 120^\circ$$

“Ideal” chains

$$U(\theta) = \begin{cases} -\varepsilon & \theta < \theta_{\max} \\ 0 & \theta > \theta_{\max} \end{cases}$$

$$0 \leq \theta \leq 120^\circ$$

# Computational model



Hard spheres

+

$$U(\theta) = \begin{cases} -\varepsilon & \theta < \theta_{\max} \\ 0 & \theta > \theta_{\max} \end{cases}$$

$$0 \leq \theta \leq 120^\circ$$

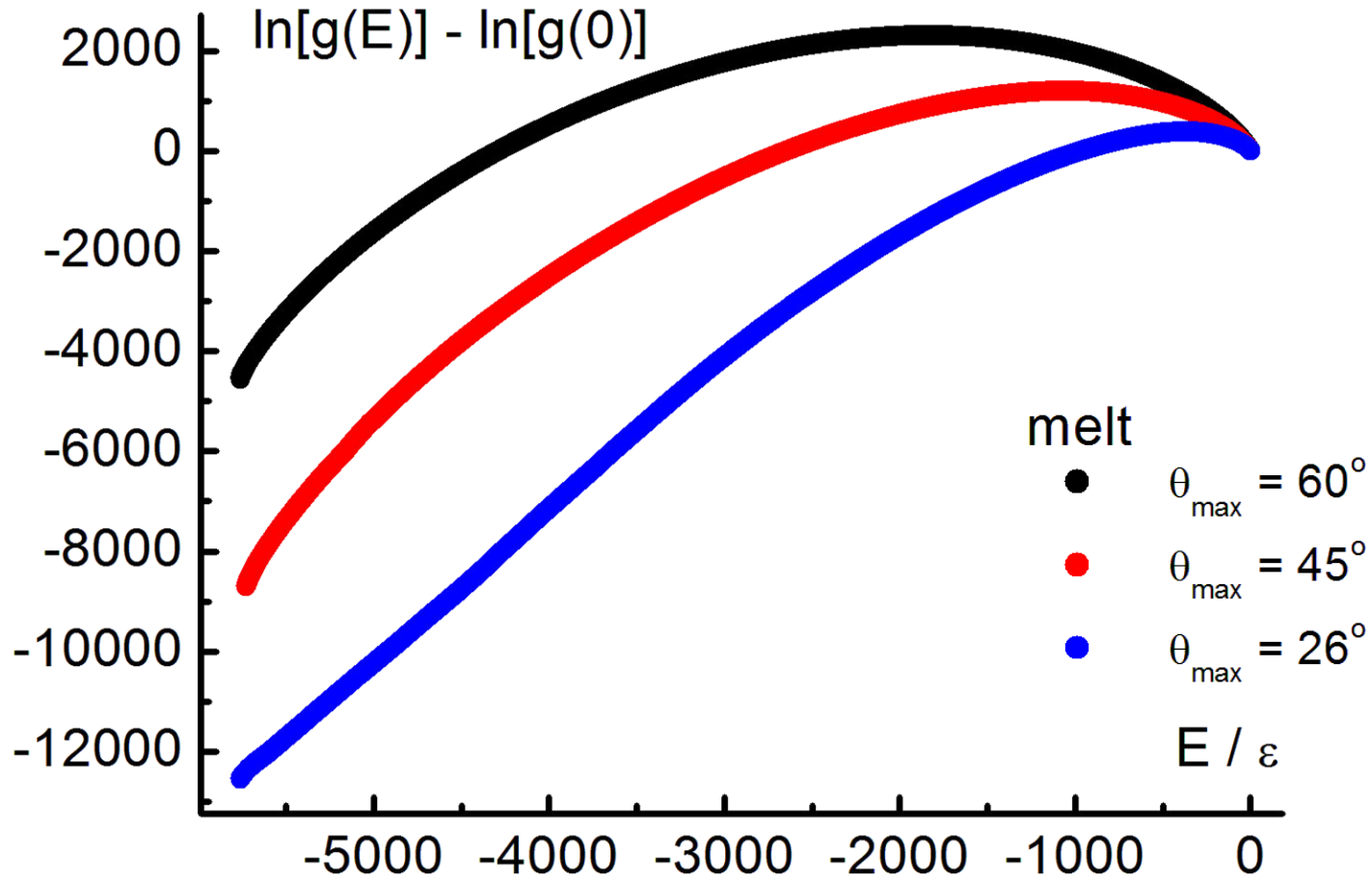
“Ideal” chains

$$U(\theta) = \begin{cases} -\varepsilon & \theta < \theta_{\max} \\ 0 & \theta > \theta_{\max} \end{cases}$$

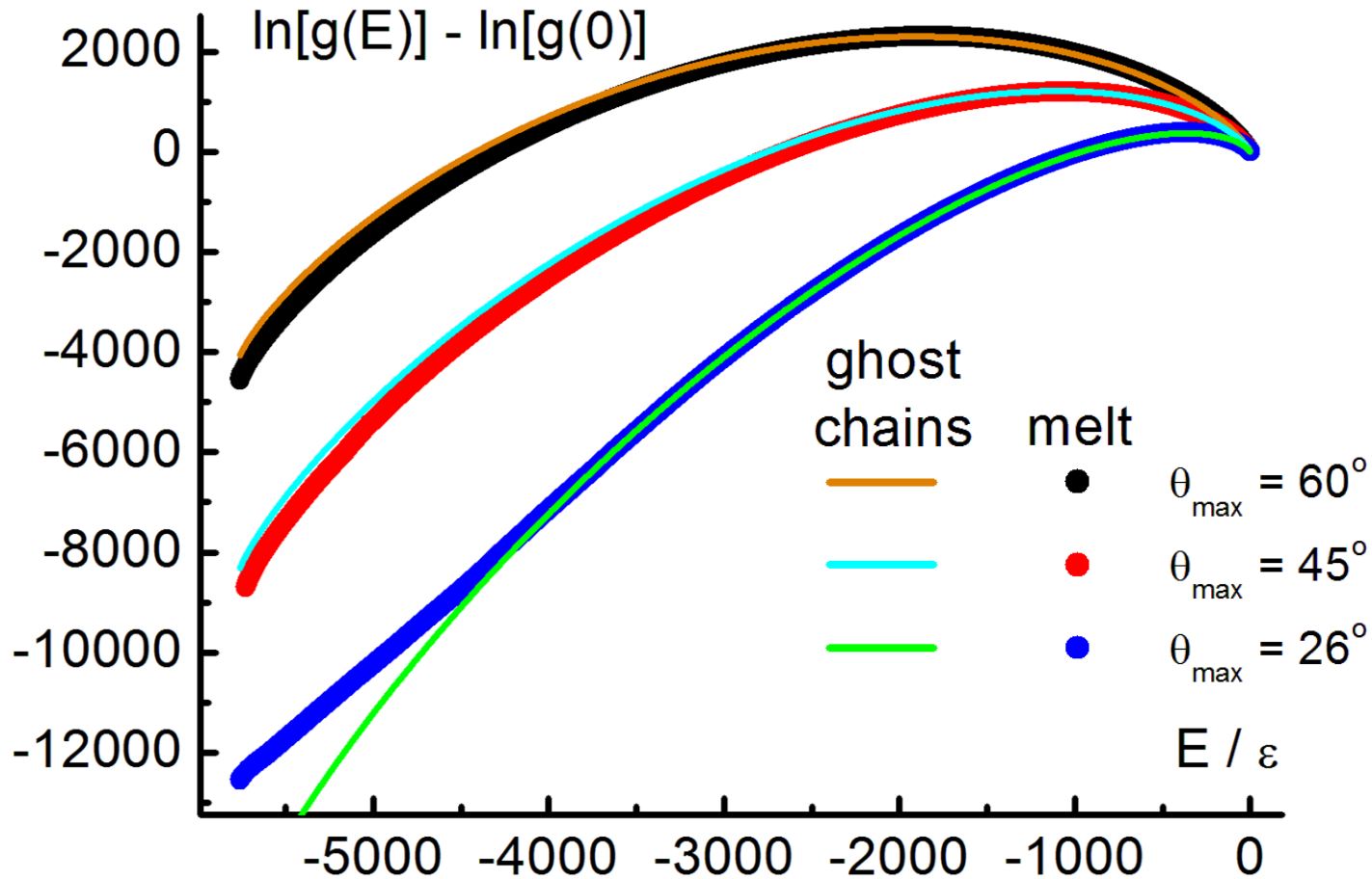
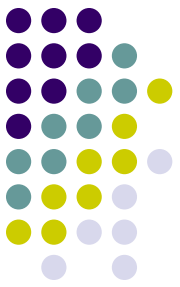
$$\hat{g}(E) \propto \binom{N_E}{|E|} p^{|E|} (1-p)^{N_E-|E|}$$

$$0 \leq \theta \leq 120^\circ$$

# Density of states

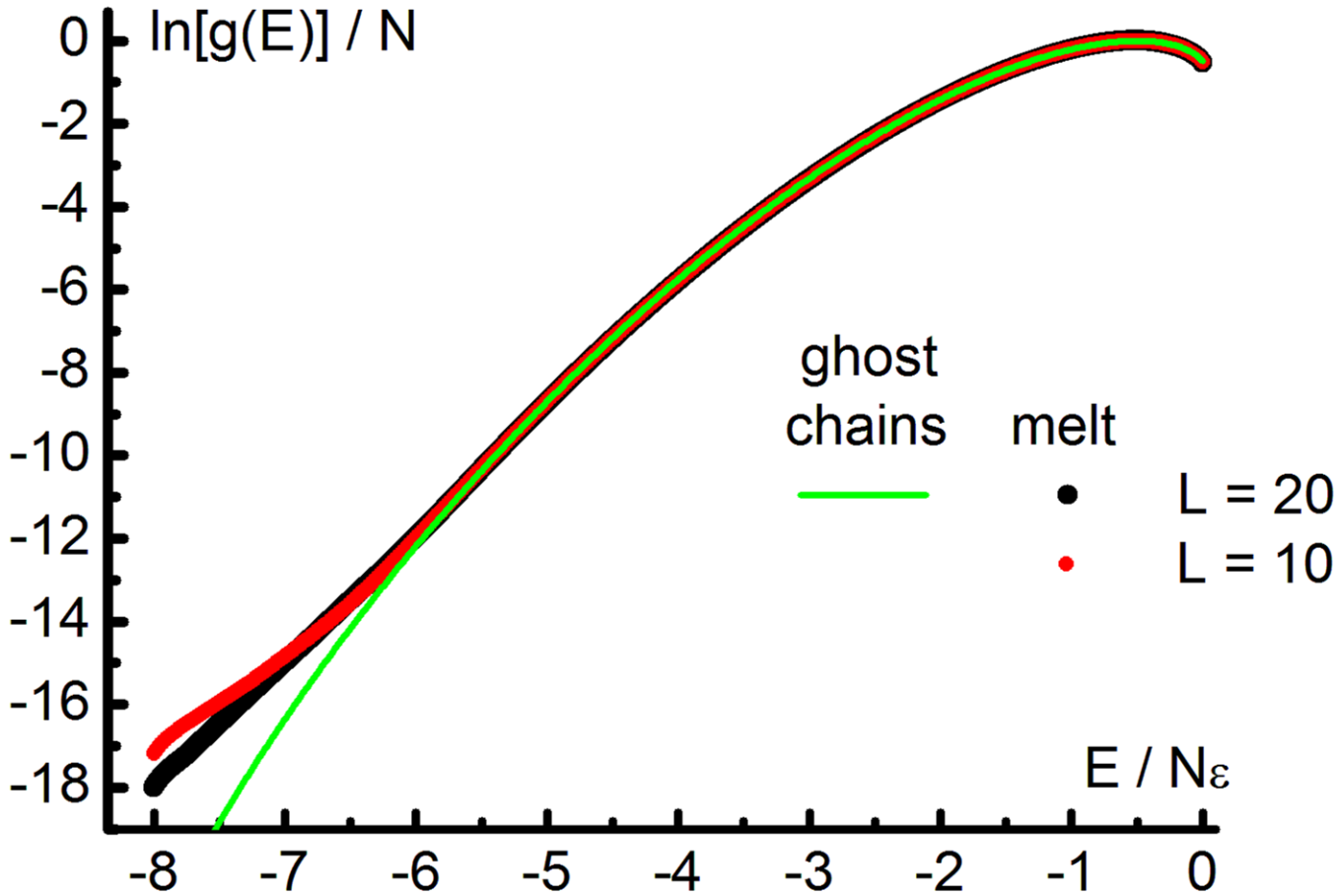
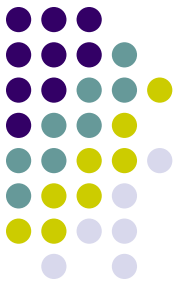


# Density of states

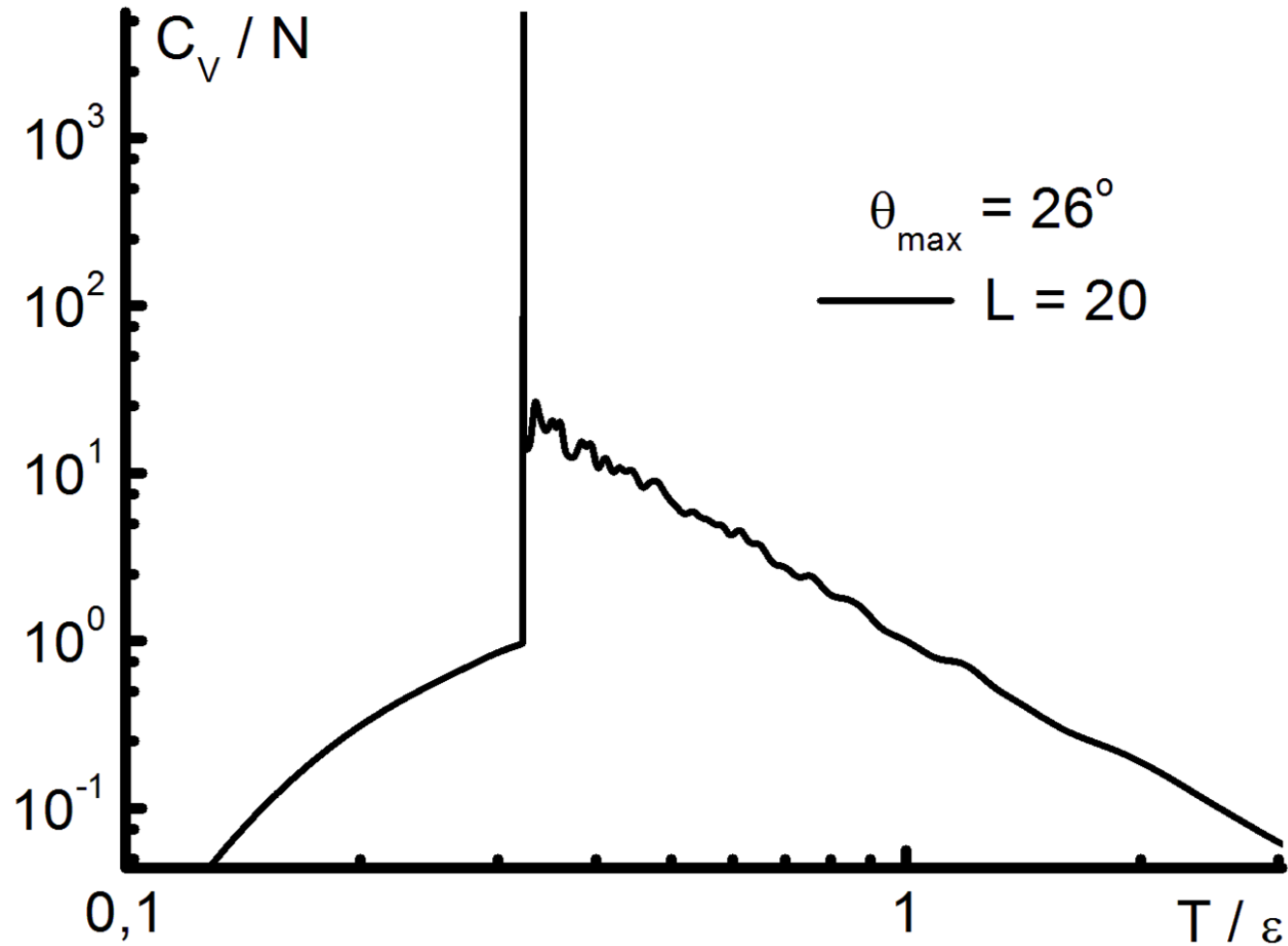
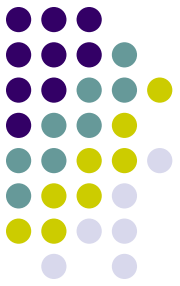




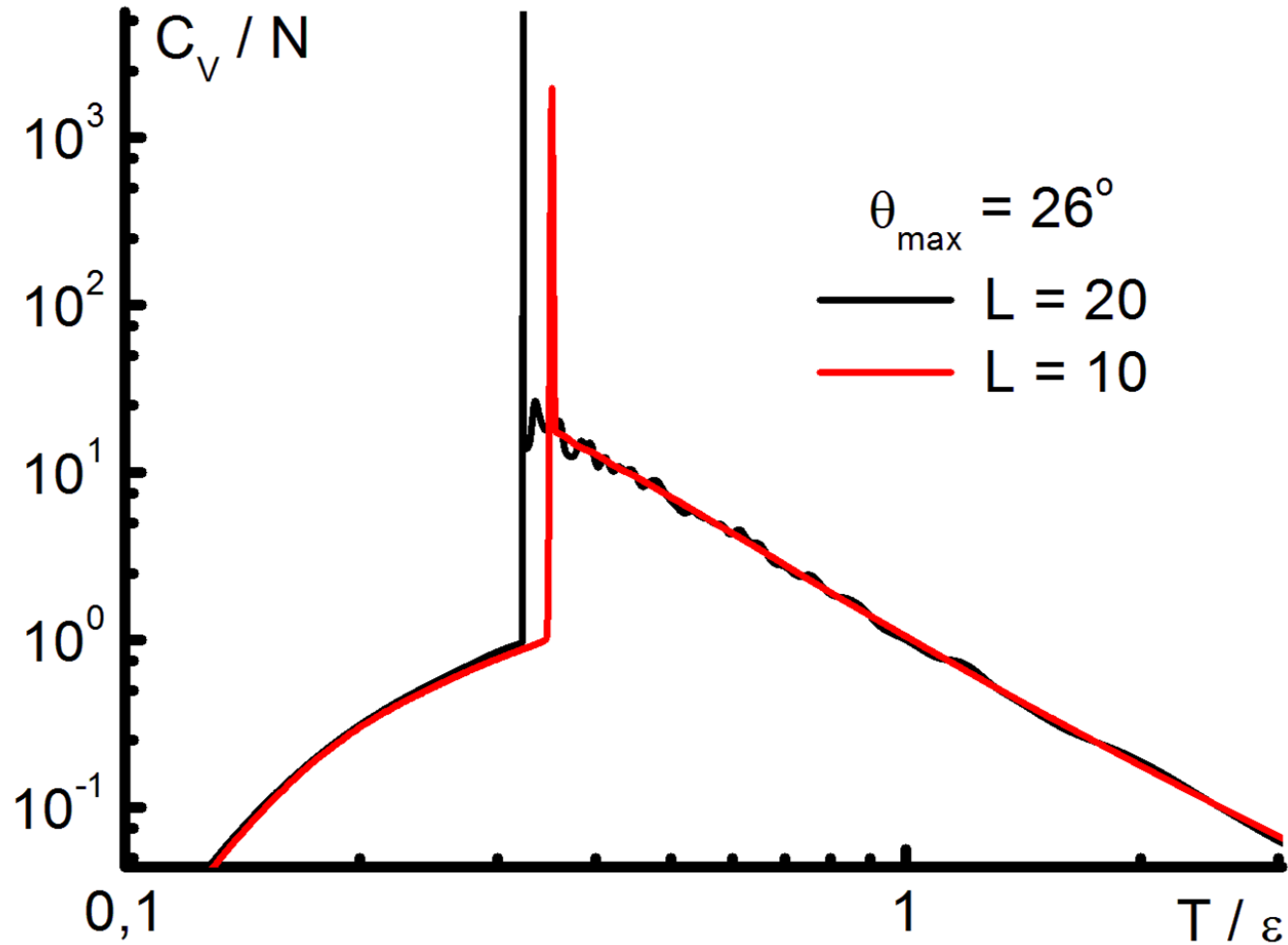
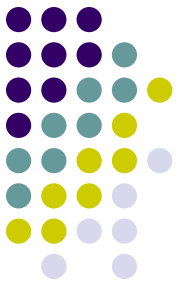
# Density of states. Stiff chains



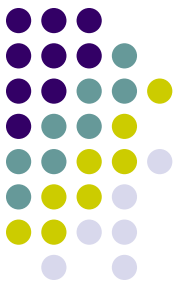
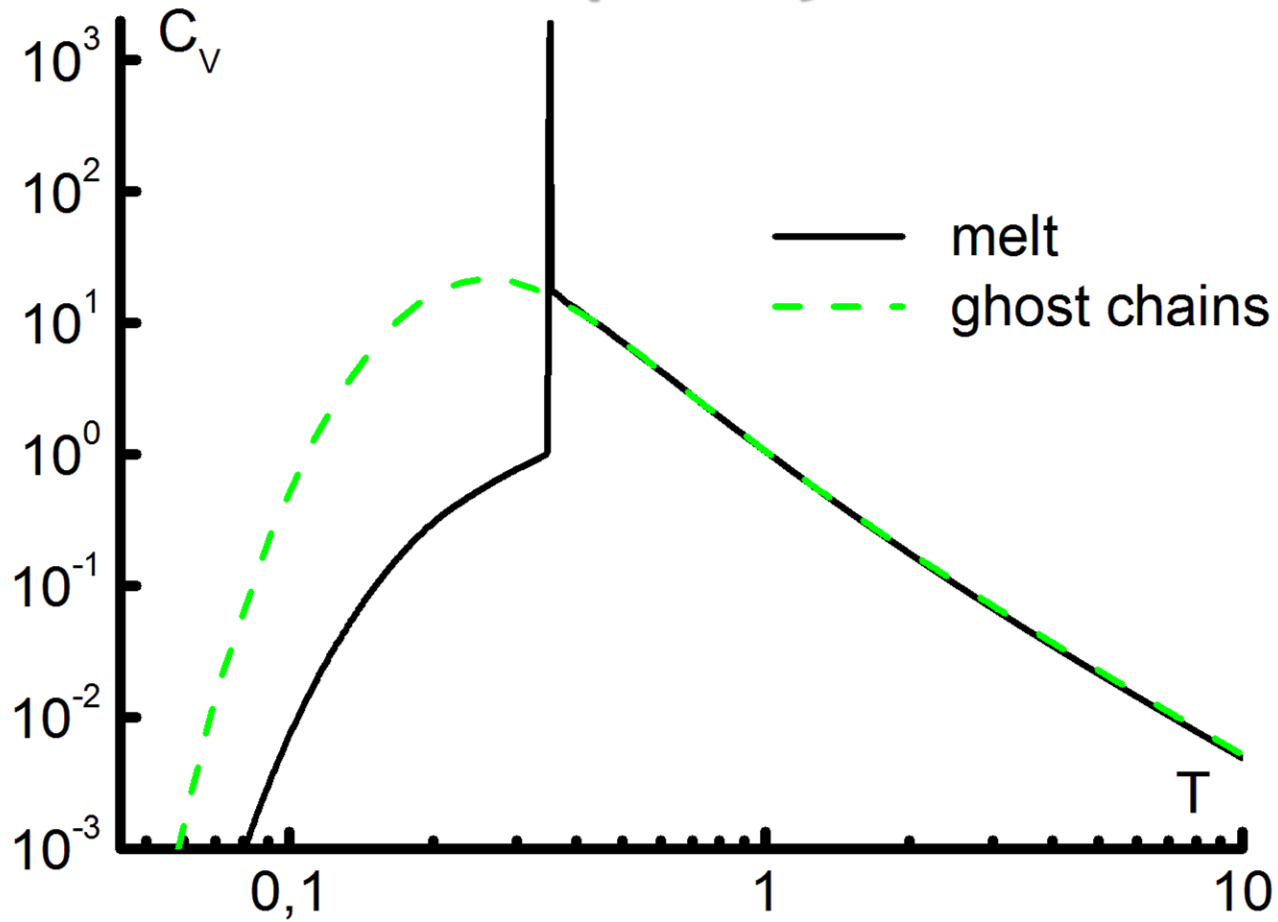
# Size effects. Heat capacity



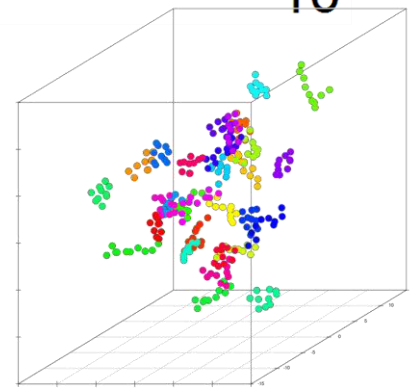
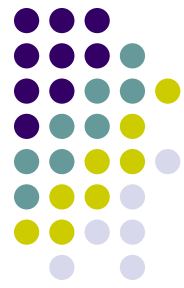
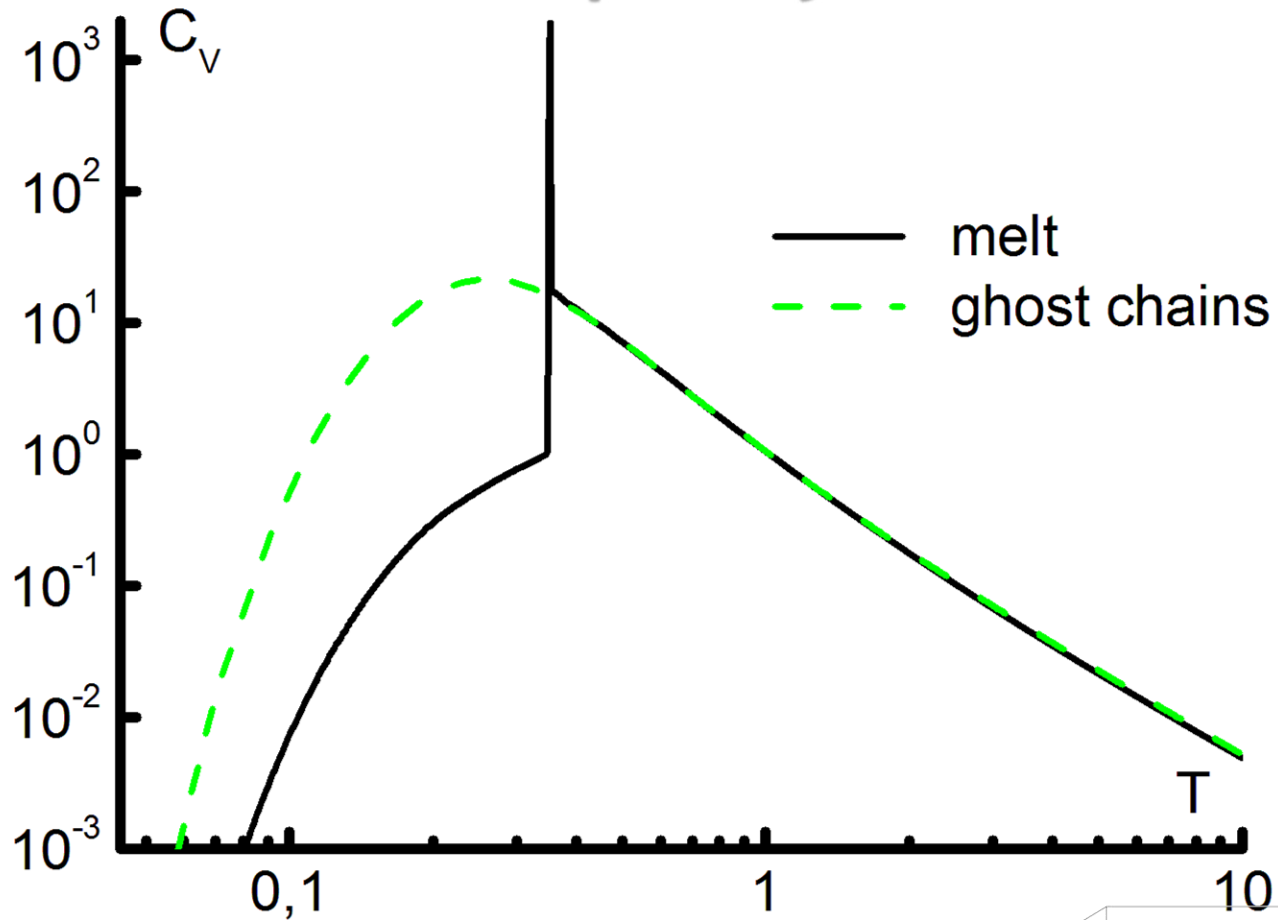
# Size effects. Heat capacity



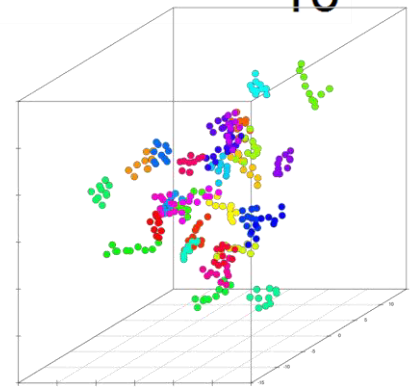
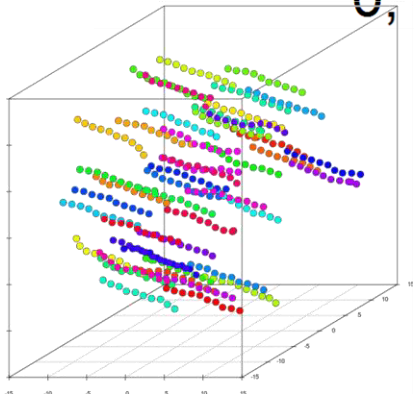
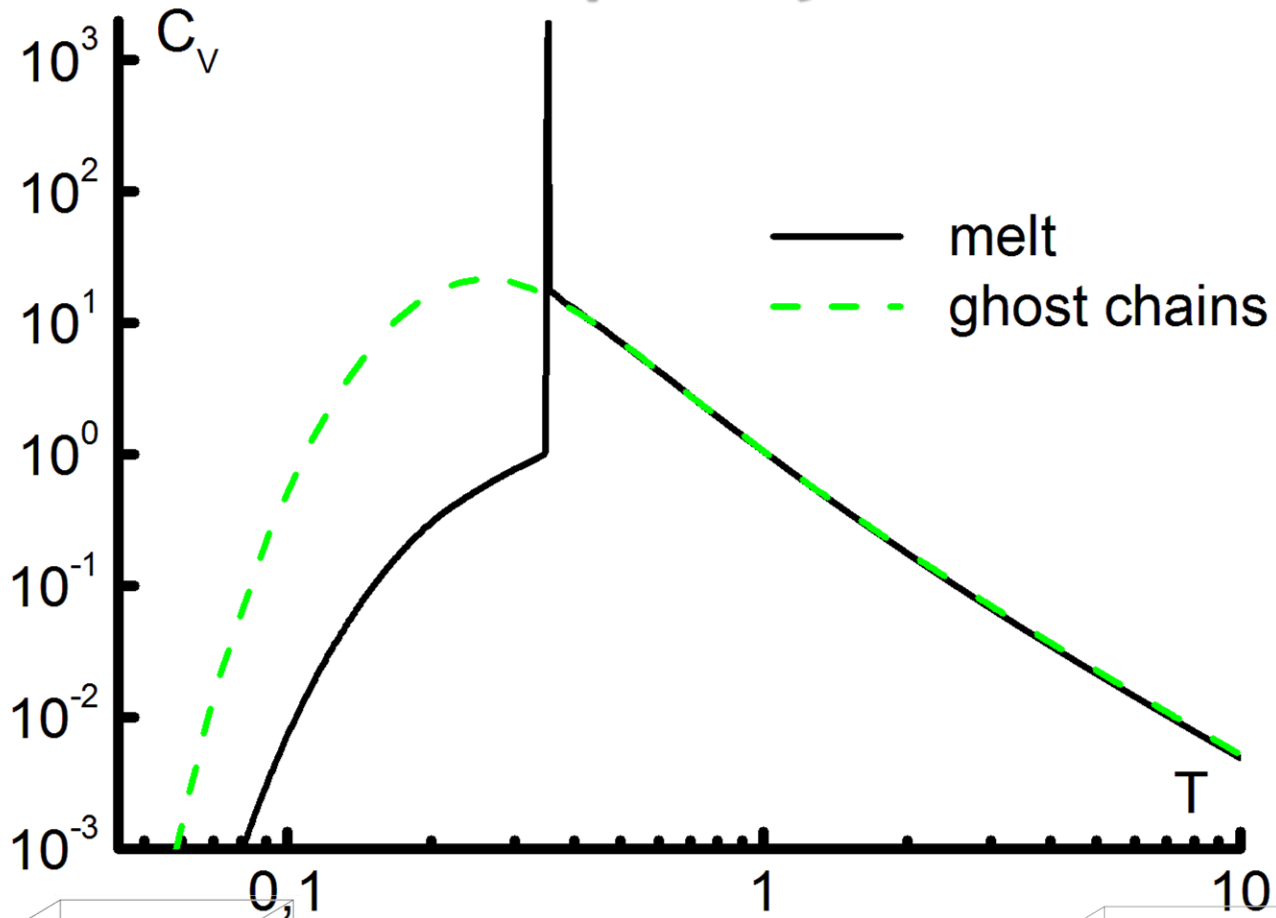
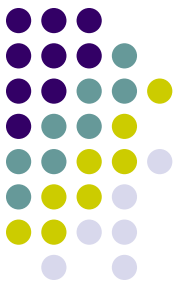
# Heat capacity



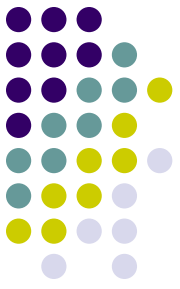
# Heat capacity



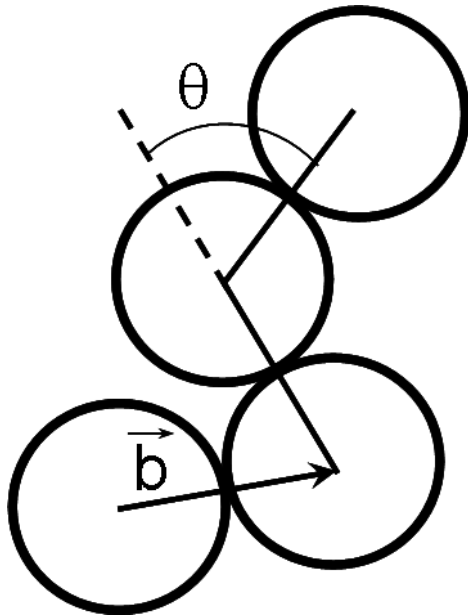
# Heat capacity



# Order parameter. Definition

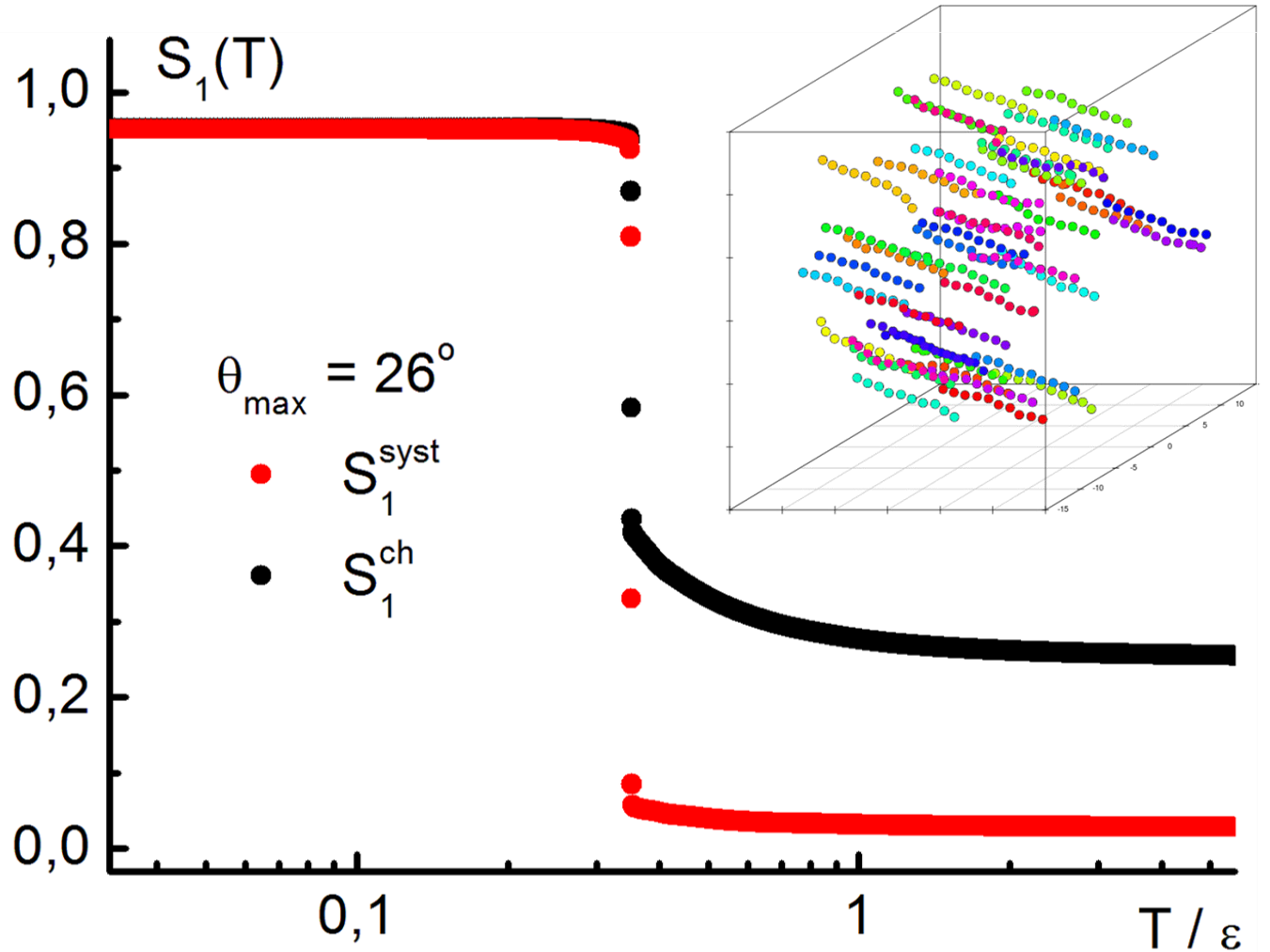
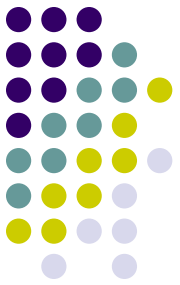


$$Q_{\alpha\beta} = \frac{1}{N} \sum_i \frac{3b_{i\alpha}b_{i\beta} - \delta_{\alpha\beta}}{2}$$



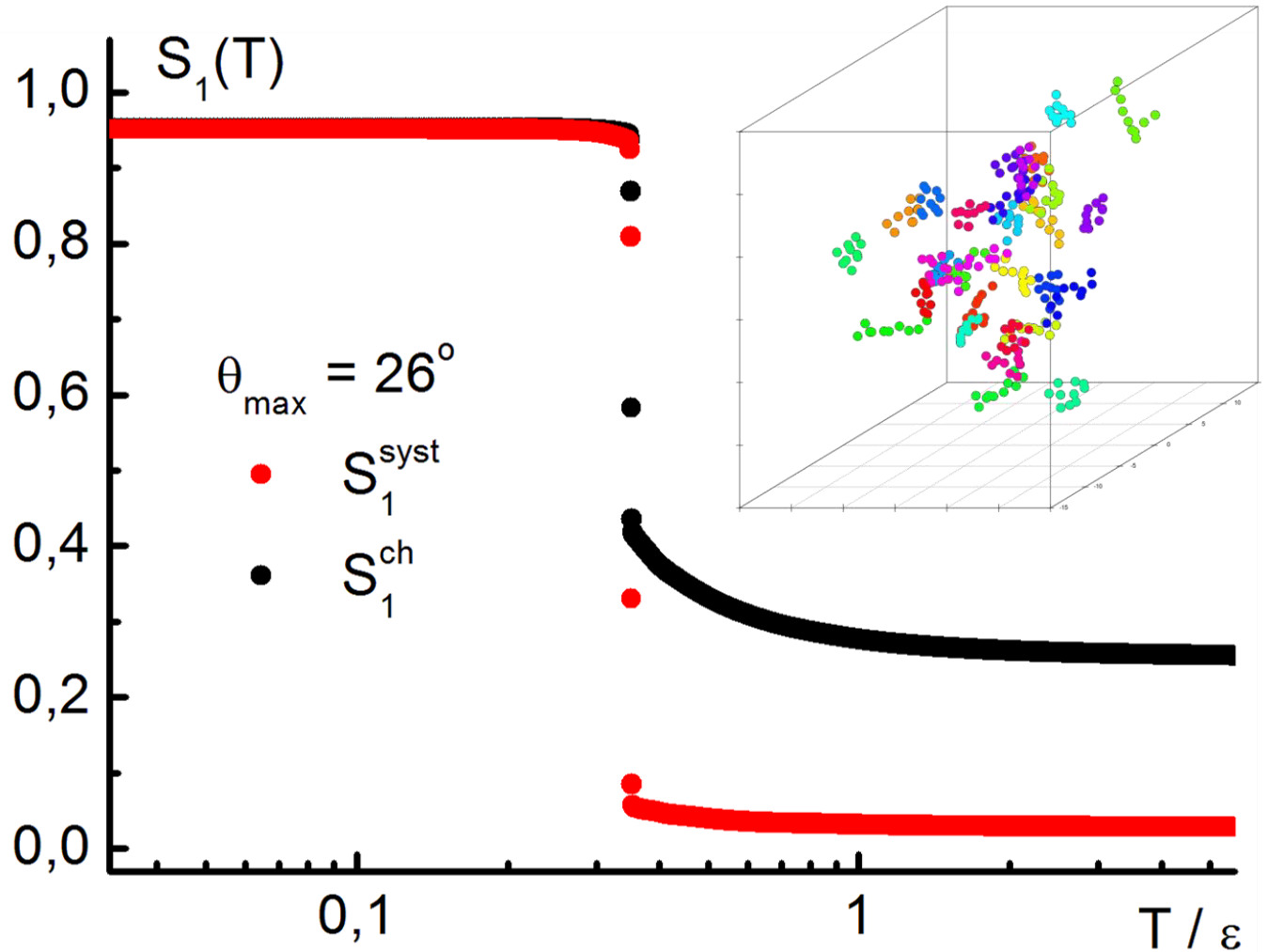
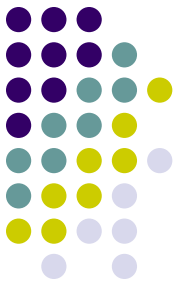
$$S_1 = \max(\det(Q_{\alpha\beta} - S_i \delta_{\alpha\beta}) = 0)$$

# Order parameter. Temperature dependence

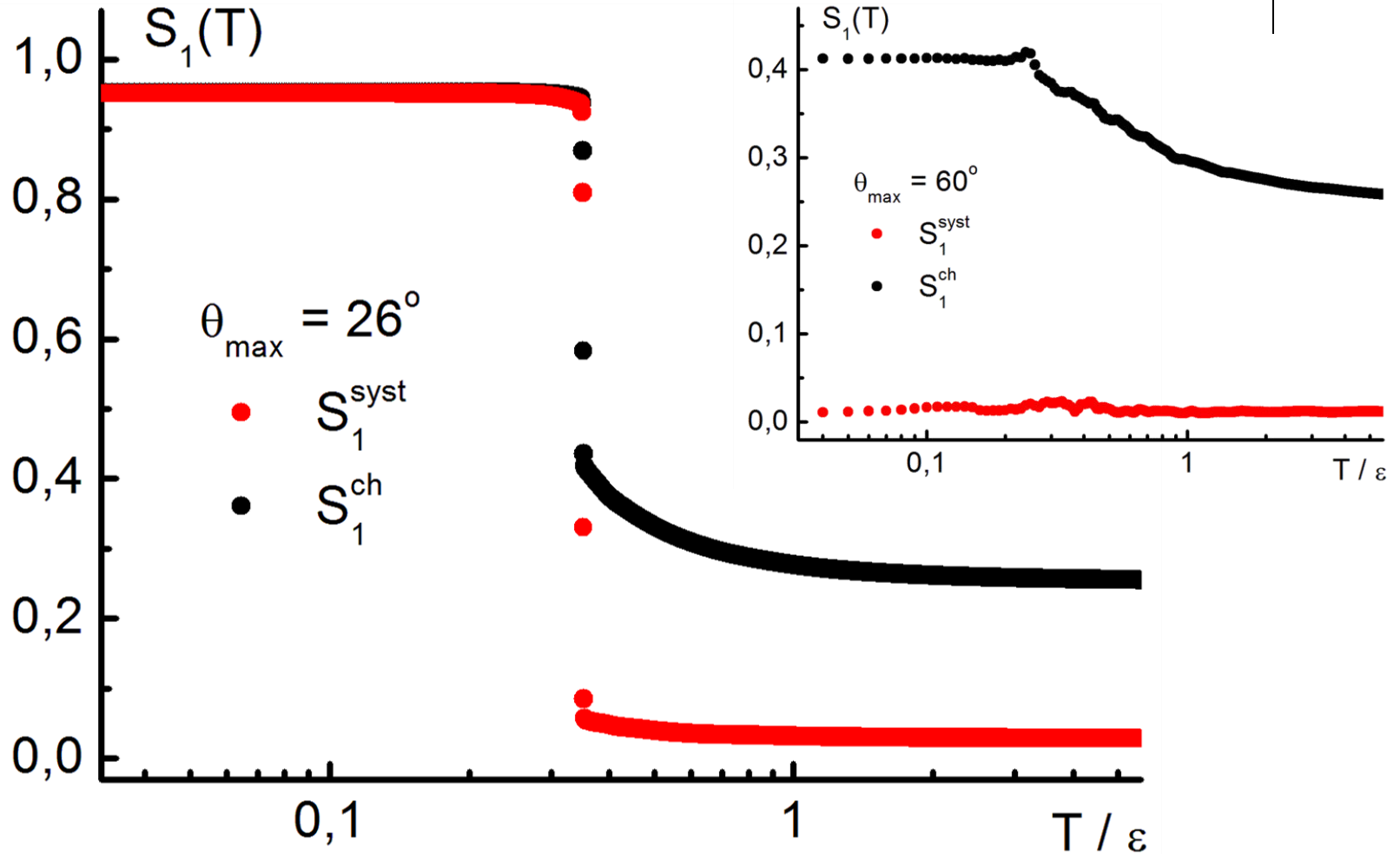
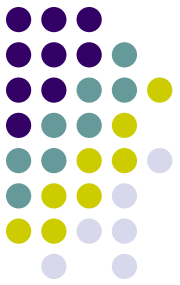




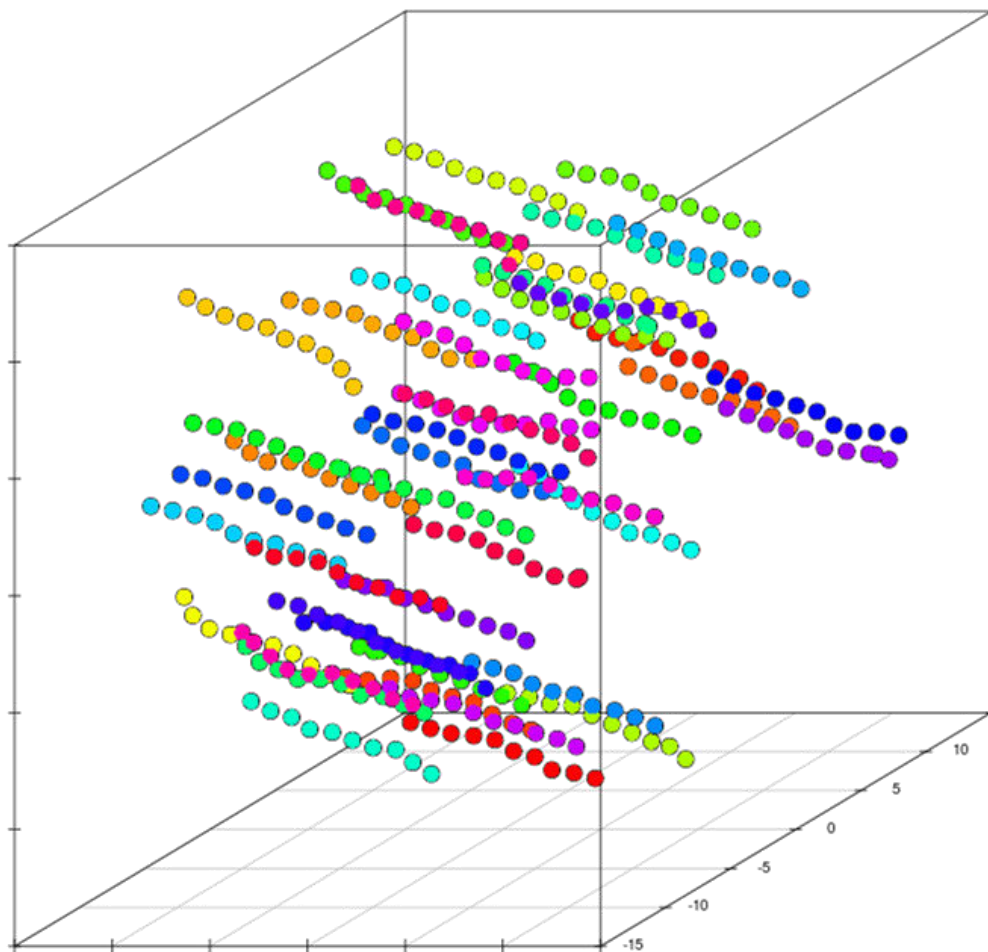
# Order parameter. Temperature dependence



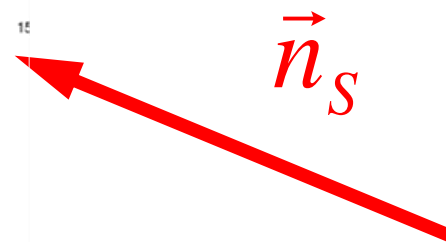
# Order parameter. Temperature dependence



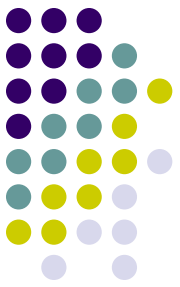
# Order parameter and density distribution



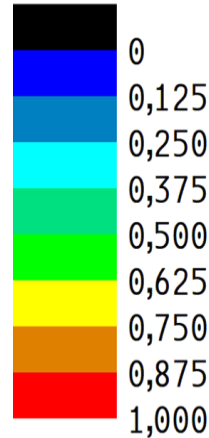
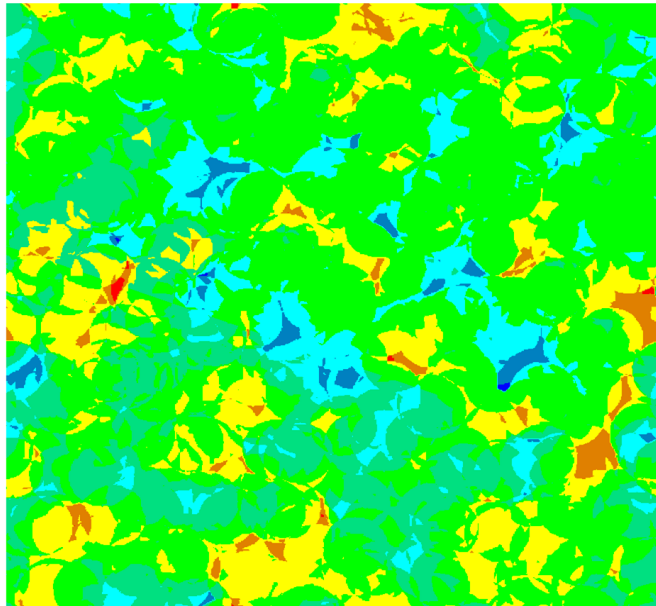
$$\left| \left( \vec{n}_S \cdot \vec{b} \right) \right|$$



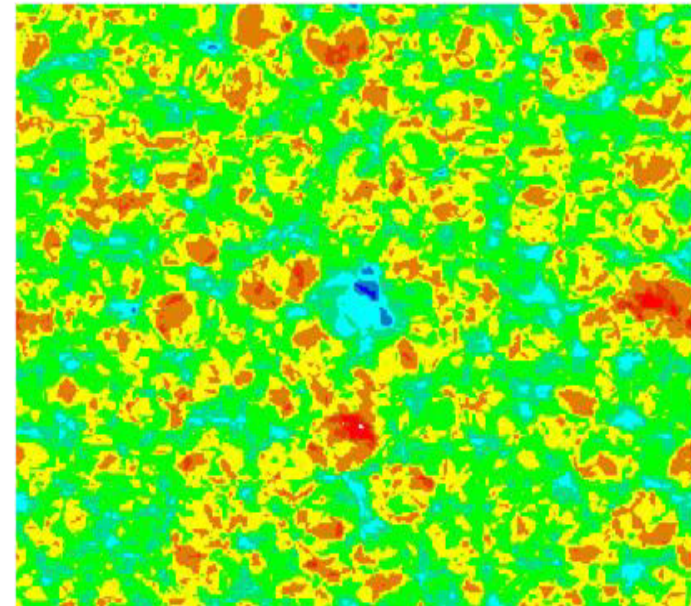
# Order parameter and density distributions. High energies



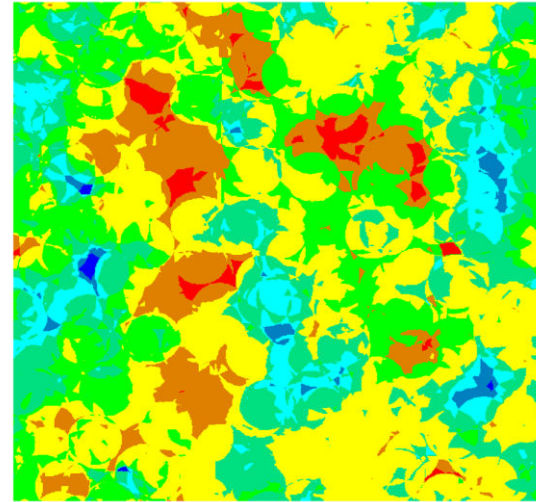
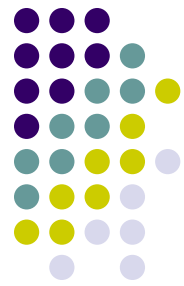
Orientation



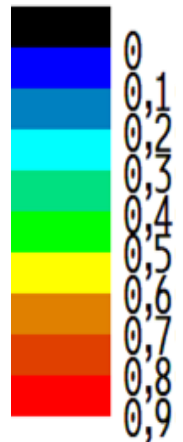
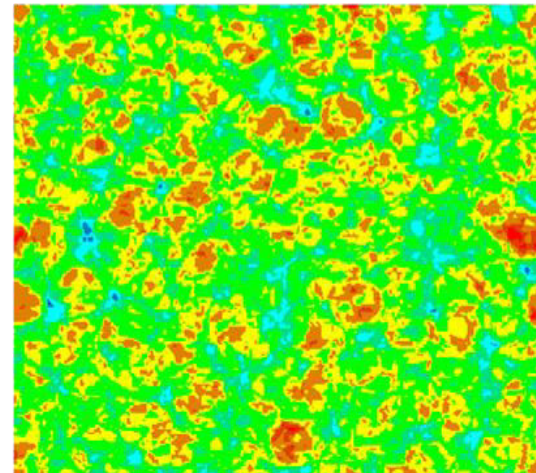
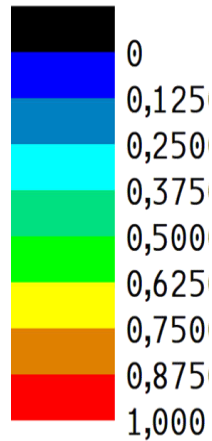
Density



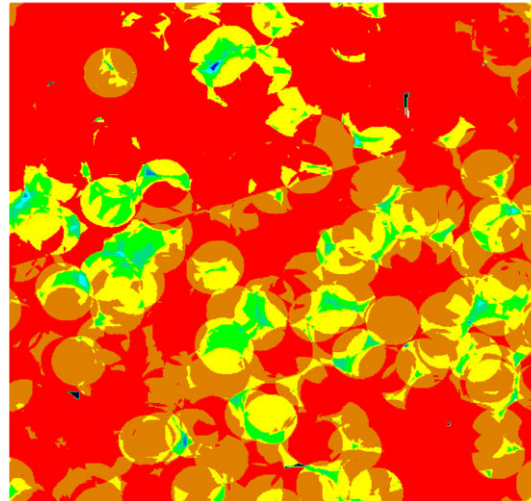
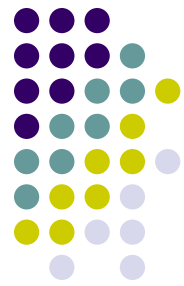
# Order parameter and density distributions. Phase transition



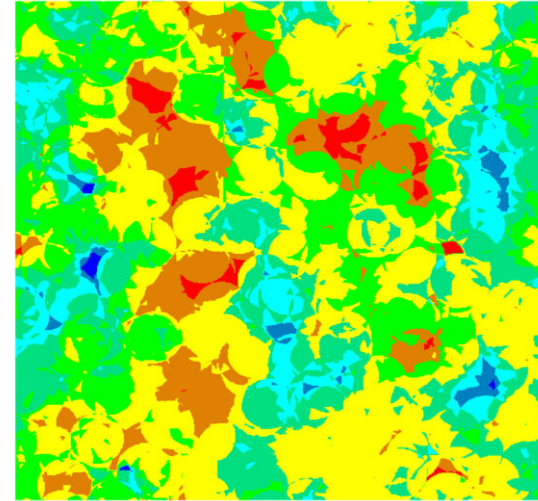
$E = -517$



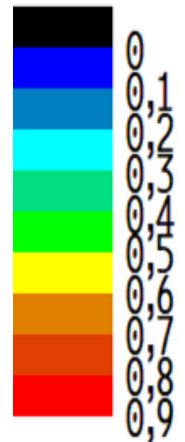
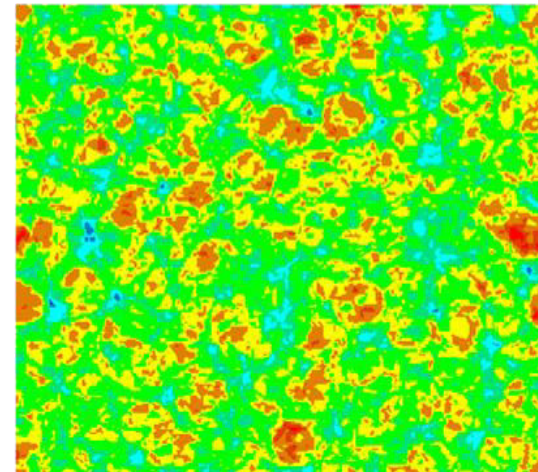
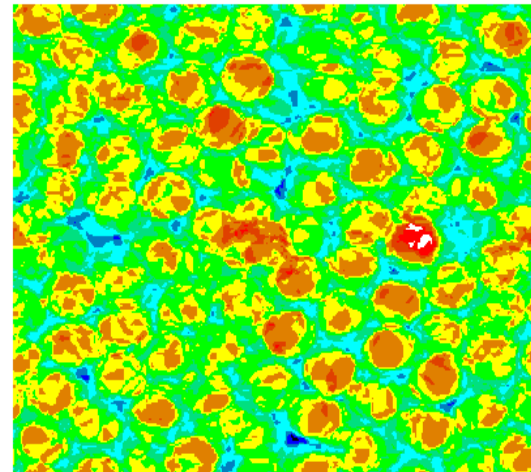
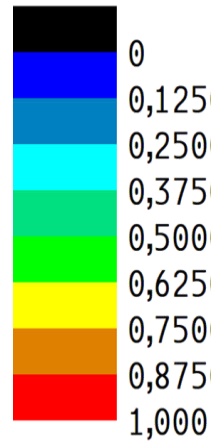
# Order parameter and density distributions. Phase transition



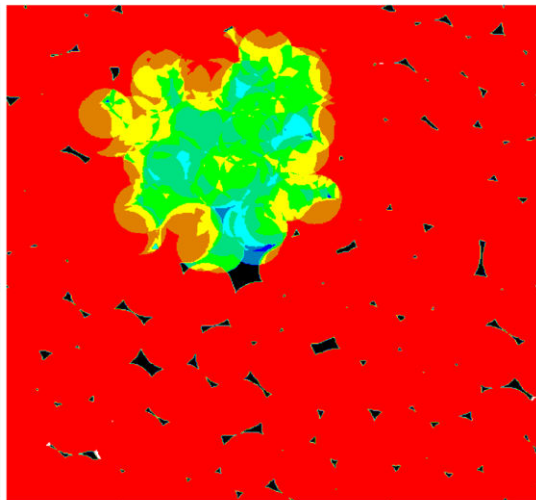
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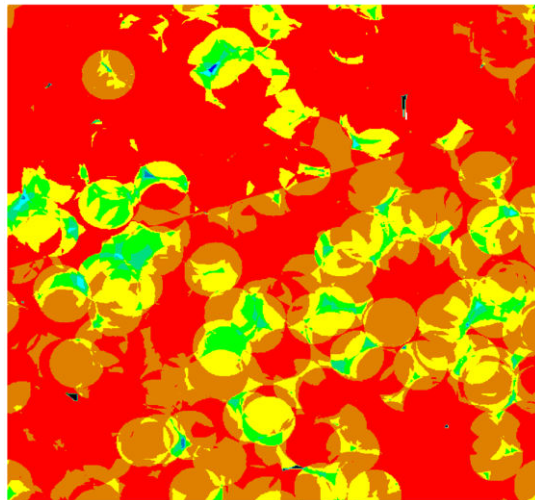
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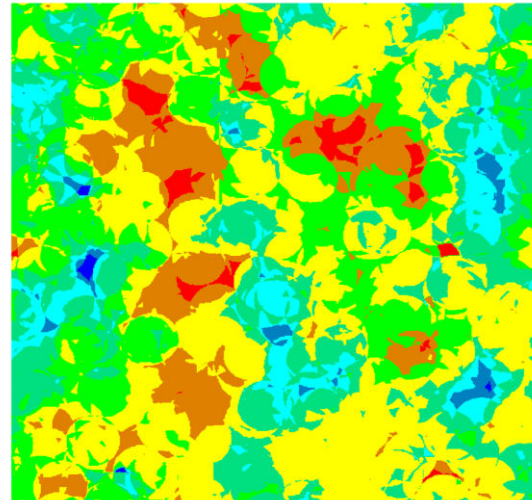
# Order parameter and density distributions. Phase transition



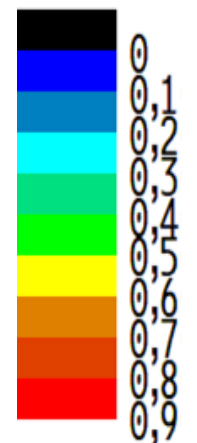
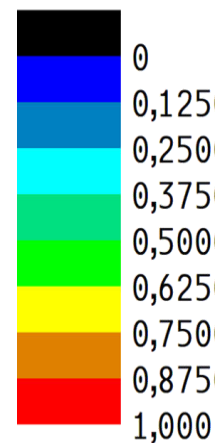
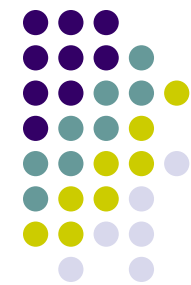
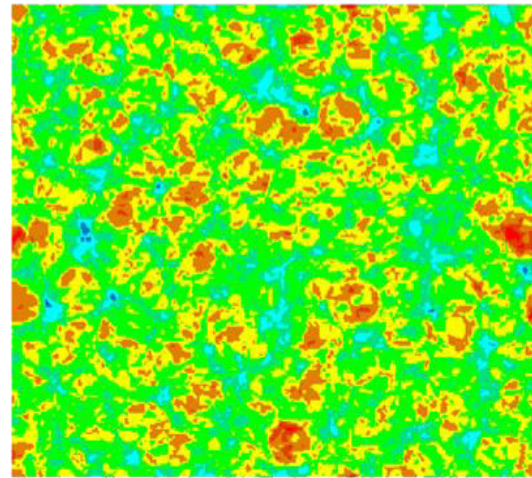
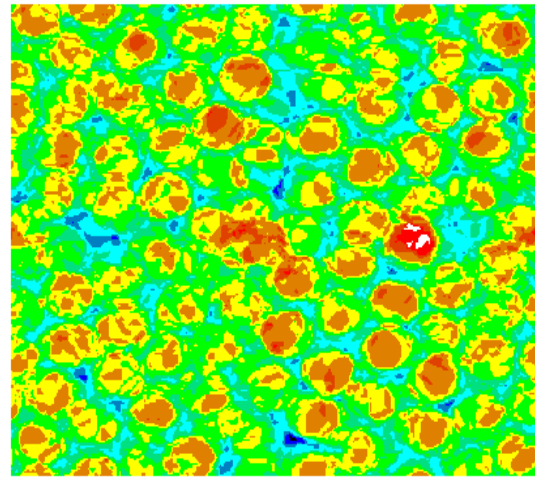
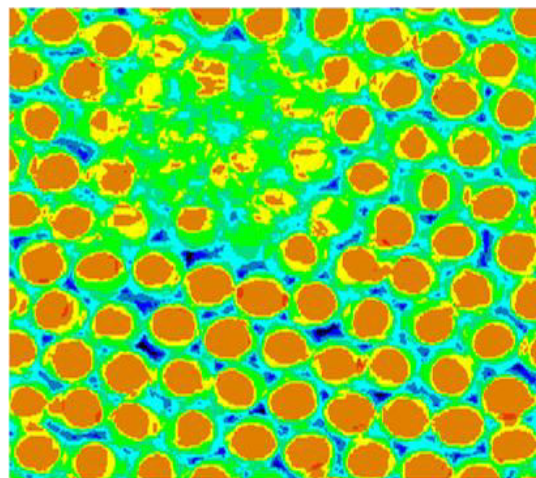
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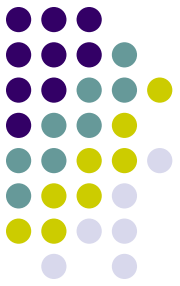
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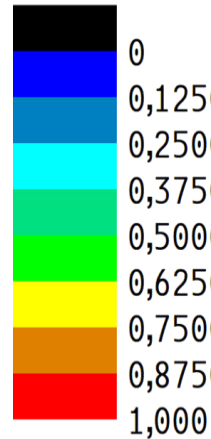
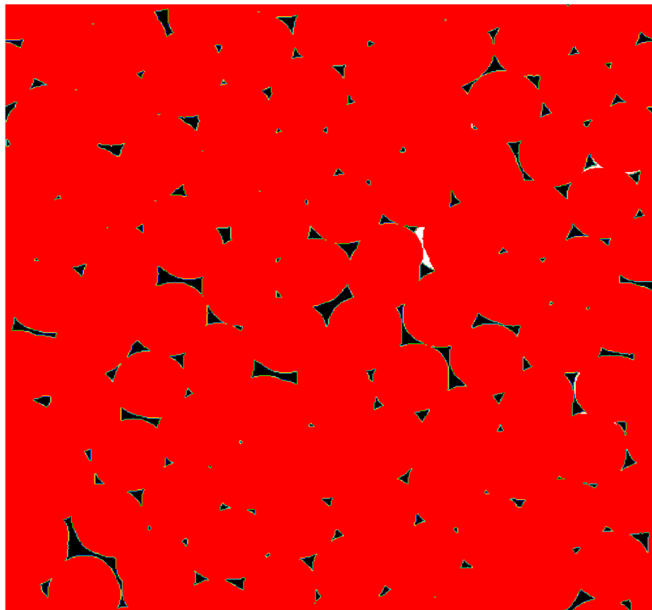
$E = -517$



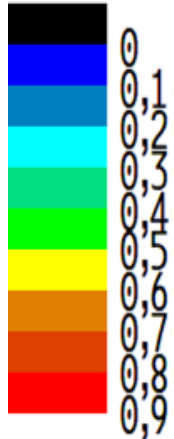
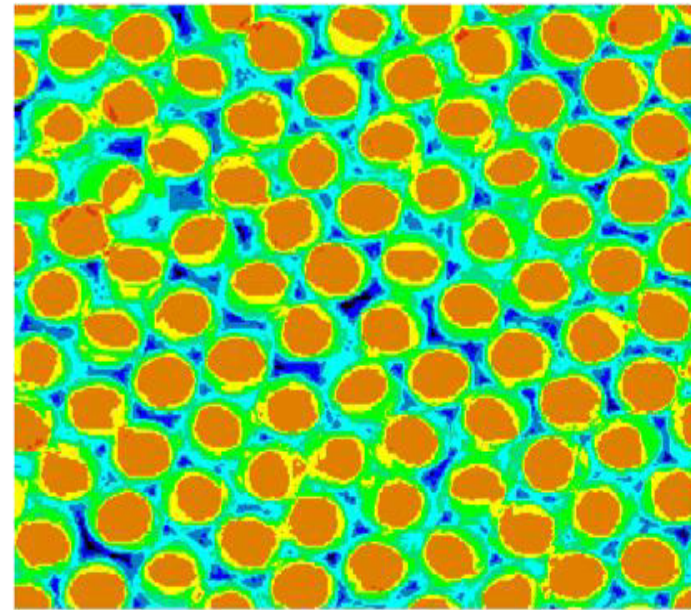
# Order parameter and density distributions. Low energies



Orientation

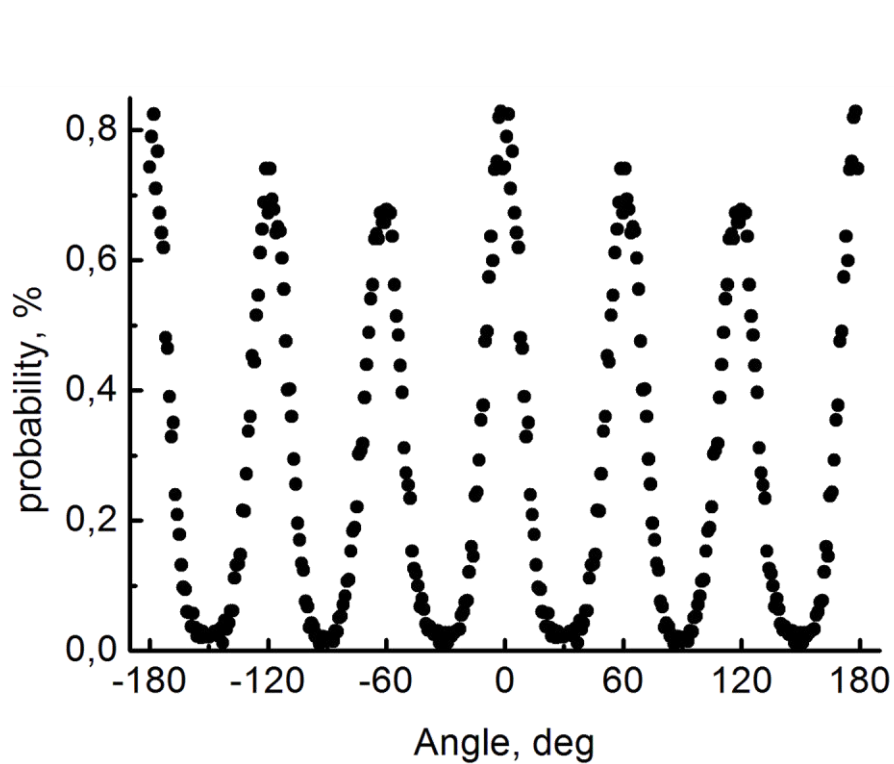


Density

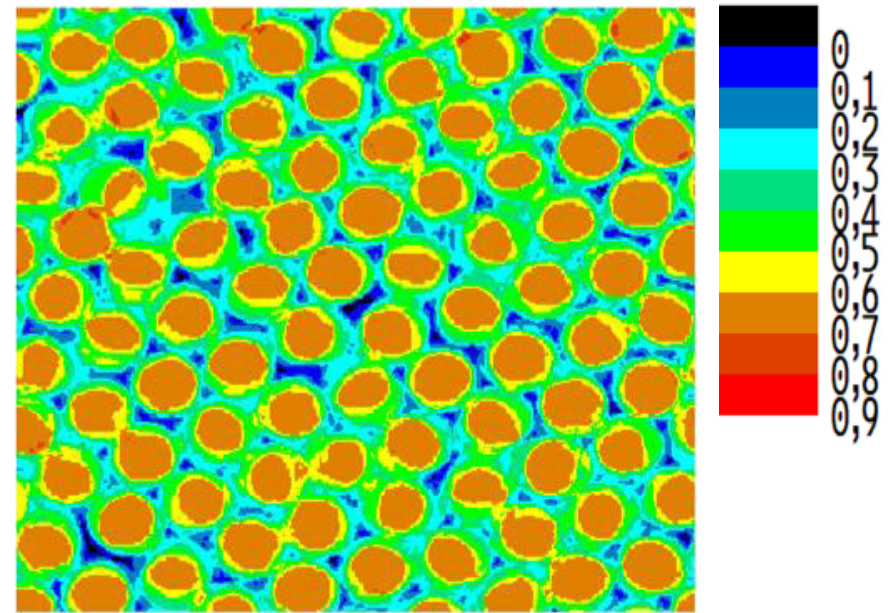




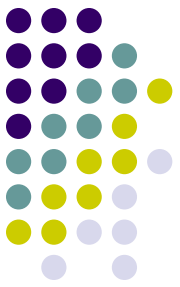
# Order parameter and density distributions. Low energies



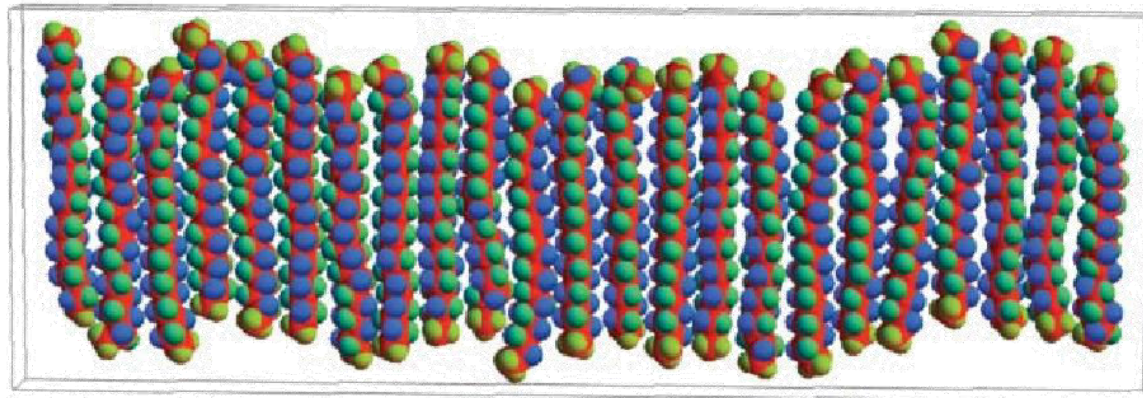
Density



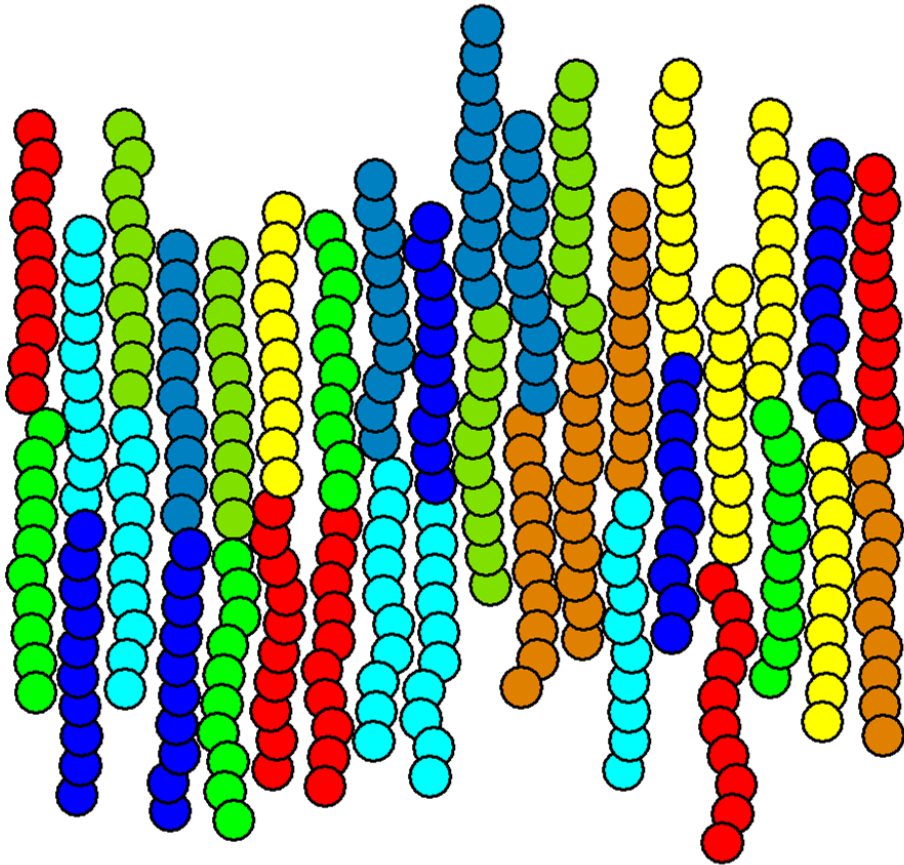
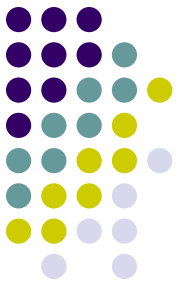
# Rotator-like phase



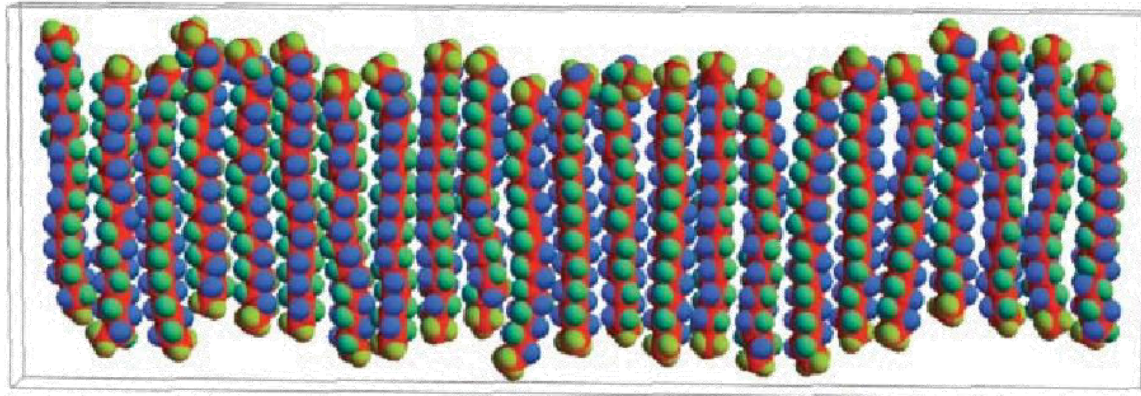
Rotator II phase



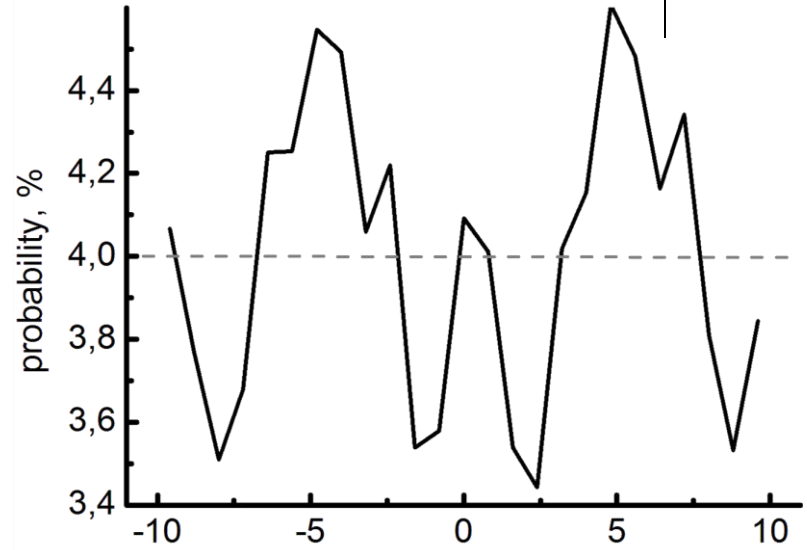
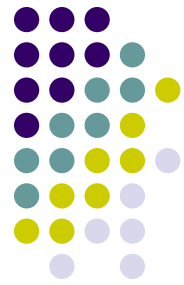
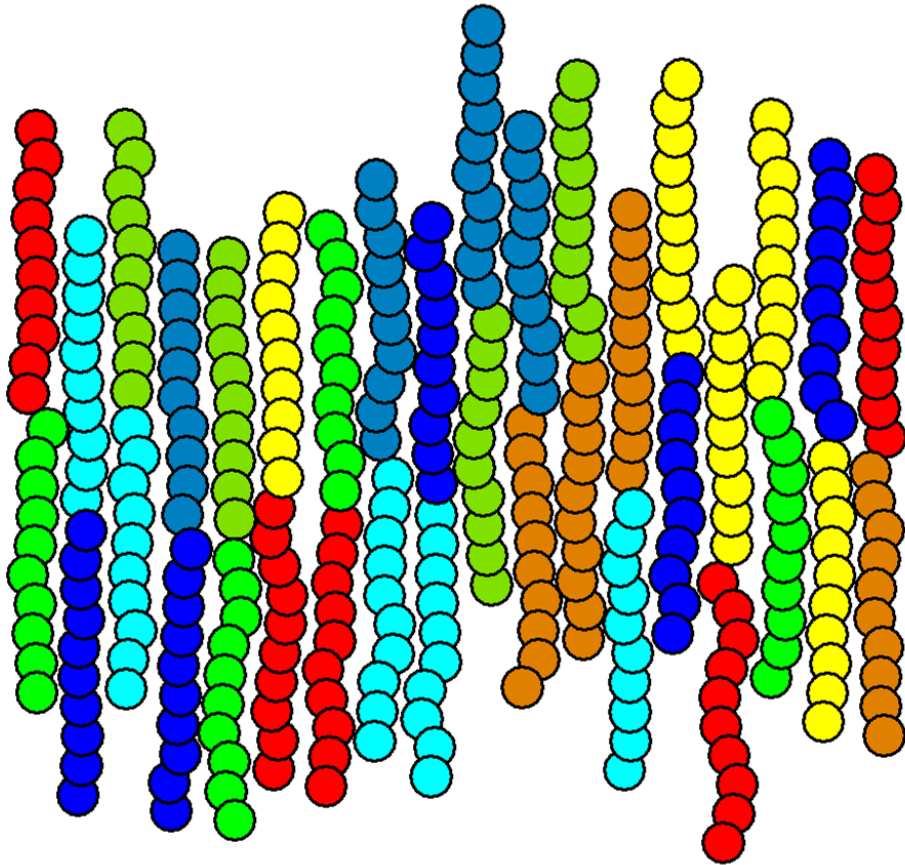
# Rotator-like phase



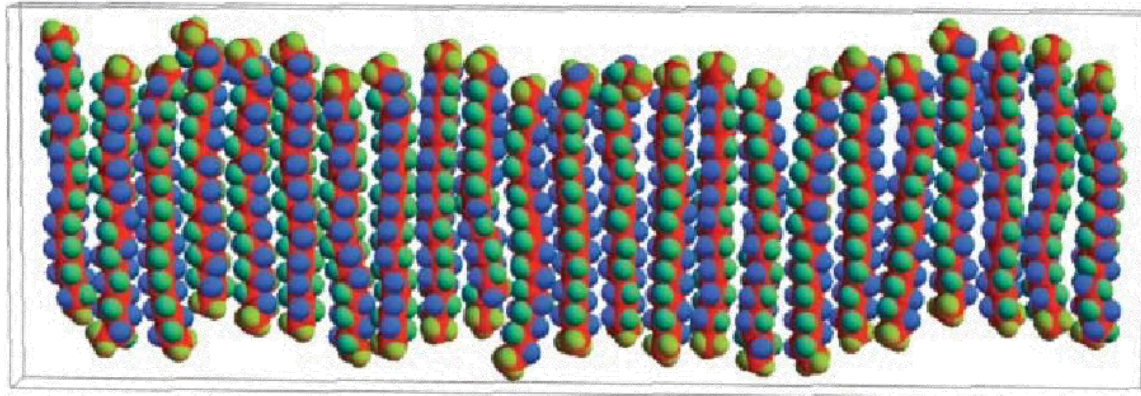
Rotator II phase



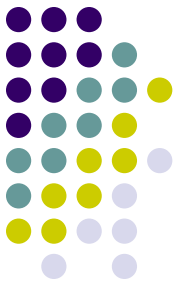
# Rotator-like phase



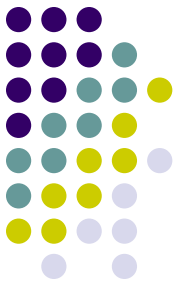
Rotator II phase



# Conclusion



- **System of stiff hard-sphere polymers has rotator-like phase**
- **WL is usable for simulations of phase transitions of polymer melts at thermodynamically equilibrium**



**Thank you for your attention!**